# Global Distance-distributions Separation for Unsupervised Person Re-identification (Supplementary Material)

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# 1 Mathematical Analysis of the Rationality of Momentum Update Mechanism

In order to mathematically prove the rationality of our momentum update design as described in Section 3.1 of the main manuscript, we design a toy game to present the momentum update process of the distance-distributions for different sample pair sets (*i.e.*, mean  $\mu$ , variance  $\sigma^2$ ) with analysis/derivation.

Assume two random sets  $\mathcal{A}, \mathcal{B}$  with N and M sample pairs, respectively, and both sets exhibit Gaussian distribution. The mean and variance of set  $\mathcal{A} = \{d_i | i = 1, \cdots, N\}$  with N sample pairs are represented as  $\mu_A = \frac{1}{N} \sum_{i=1}^N d_i$ ,  $\sigma_A^2 = \frac{1}{N} \sum_{i=1}^N (d_i - \mu_A)^2$  while those of set  $\mathcal{B} = \{d'_j | j = 1, \cdots, M\}$  with Msample pairs are estimated by  $\mu_B = \frac{1}{M} \sum_{j=1}^M d'_j, \sigma_B^2 = \frac{1}{M} \sum_{j=1}^M (d'_j - \mu_B)^2$ . We represent the set  $\mathcal{C}$  as the combination of set  $\mathcal{A}$  and set  $\mathcal{B}$ , the mean of the combined set  $\mathcal{C}$  can be formulated as:

$$\mu_C = \frac{\sum_{i=1}^N d_i + \sum_{j=1}^M d'_j}{N+M} = \frac{N}{N+M} \mu_A + \frac{M}{N+M} \mu_B = \beta \mu_A + (1-\beta)\mu_B,$$
(1)

where  $\beta = \frac{N}{N+M}$ . Similarly, the variance of the combined set C can be obtained:

$$\sigma_C^2 = \frac{\sum_{i=1}^N (d_i - \mu_C)^2 + \sum_{j=1}^M (d'_j - \mu_C)^2}{N + M},$$
(2)

when N is much larger than M (just like the situation in our training where the number of the previously "seen" mini-batches/samples is much larger than the number of samples in the current mini-batch), we could use  $\mu_A$  to approximate

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Datasets	Abbreviation	Identities	Images	Cameras	Scene				
Market1501 [25]	M	1501	32668	6	outdoor				
DukeMTMC-reID [26]	D	1404	32948	8	outdoor				
CUHK03 [9]	C	1467	28192	2	indoor				
MSMT17 [18]	MSMT17	4101	126142	15	outdoor, indoor				

Table 1: Details about the ReID datasets.

 $\mu_C$ , *i.e.*,  $\mu_C \approx \mu_A$ , thus we can have:

$$\sigma_C^2 \approx \frac{\sum_{i=1}^N (d_i - \mu_A)^2 + \sum_{j=1}^M (d'_j - \mu_A)^2}{N + M}$$

$$= \frac{N}{N + M} \sigma_A^2 + \frac{M}{N + M} \frac{\sum_{j=1}^M (d'_j - \mu_A)^2}{M}$$

$$= \beta \sigma_A^2 + (1 - \beta) \frac{\sum_{j=1}^M (d'_j - \mu_A)^2}{M}.$$
(3)

By taking the sample pairs within a min-batch as the sample pairs of set  $\mathcal{B}$ , we can see that our momentum update design in Eq. (1) of our main manuscript is consistent with the above analysis/derivation.

## 2 Details of Datasets

In Table 1, we present the detailed information about the related person ReID datasets. Market1501 [25], DukeMTMC-reID [26], CUHK03 [9], and large-scale MSMT17 [18] are the most commonly used datasets for unsupervised domain adaptive person ReID [22, 23, 4] and fully supervised person ReID [24, 30]. Market1501, DukeMTMC-reID, CUHK03, and MSMT17 all have commonly used pre-established train and test splits, which we use for our training and cross dataset test (*e.g.*,  $M \rightarrow D$ ,  $D \rightarrow M$ ).

### **3** Implementation Details

**Data Augmentation and Training.** In the first stage of model pre-training, just as in [13], we use the commonly used data augmentation strategies of random cropping [17, 24], horizontal flipping, random erasing (REA) [12, 30], and the label smoothing regularization [15] to train the network for obtaining the capability of extracting discriminative features for person ReID on the labeled source dataset. The training is supervised by classification loss [14, 5] and triplet loss with batch hard mining [6]. In the second stage of *clustering*, we discard all the previous data augmentation operations and just simply extract features for the images of the target datasets for clustering. For the third stage of *adapta-*tion, consistent with the operations in the first stage, we leverage all these data augmentations to fine-tune the network.

		$M \rightarrow N$	ISMT17	$D \rightarrow MSMT17$		
Unsupervised ReID	Venue	mAP	Rank-1	mAP	Rank-1	
PTGAN [18] SSG [4]	CVPR'18 ICCV'19	$\begin{array}{c} 2.9\\ 13.2 \end{array}$	$10.2 \\ 31.6$	3.3 13.3	11.8 $32.2$	
Baseline Baseline+ <b>GDS-H</b>	This work This work	7.2 <b>14.9</b>	18.9 <b>34.3</b>	9.2 <b>14.2</b>	25.3 <b>33.9</b>	

Table 2: Performance (%) comparisons with the state-of-the-art approaches for unsupervised person ReID on the target dataset MSMT17 [18].

In the first and third stages, following [6], a batch is formed by first randomly sampling P identities. For each identity, we sample K images. Then the batch size is  $B = P \times K$ . We set P = 32 and K = 4 (*i.e.*, batch size  $B = P \times K = 128$ ). We use Adam optimizer [8] for both stages.

For the first stage of model pre-training, we set the initial learning rate to  $3 \times 10^{-4}$  and regularize the network with a weight decay of  $5 \times 10^{-4}$ . The learning rate is decayed by a factor of 0.1 for every 50 epochs. We train the model on the source dataset for a total of 150 epochs. For the third stage of *adaptation*, we set the learning rate to  $6 \times 10^{-5}$  and keep it unchanged. The second stage and the third stage are executed alternatively for 30 iterations. For each iteration, we train our model for 70 epochs (that means, traverse all the target training samples for 70 times). For our proposed schemes, on top of *Baseline*, we add the proposed GDS constraint in the third stage.

All our models are implemented on PyTorch and trained on a single 16G NVIDIA-P100 GPU. We will release our code upon acceptance.

## 4 Influence of the Hyper-parameters $\lambda_h$ and $\lambda_{\sigma}$

The hyper-parameter  $\lambda_h$  is used to balance the importance between the basic GDS loss  $\mathcal{L}_{GDS}$  and the distribution-based hard mining loss  $\mathcal{L}_H$ .  $\lambda_{\sigma}$  aims to balance the mean and variance constraints within  $\mathcal{L}_{GDS}$ . For  $\lambda_h$  and  $\lambda_{\sigma}$ , we initially set them to 1, and then coarsely determine each one based on the corresponding loss values and their gradients observed during the training. The decision principle is to set their values to make the loss values/gradients lie in a similar range. Grid search within a small range of the derived  $\lambda_h/\lambda_{\sigma}$  is further employed to get better parameters. Actually, we observed the final performance is not very sensitive to the two hyper-parameters, we experimentally set  $\lambda_h = 0.5, \lambda_{\sigma} = 1.0$  in the end.

### 5 Comparison with State-of-the-Arts (Complete Version)

More comparison results with state-of-the-art methods on the target dataset MSMT17 can be found in Table 2. We observe that in comparison with *Base-line*, our GDS constraint brings gains of 7.7%/15.4% and 5.0%/8.6% in

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Table 3: Performance (%) comparisons with the state-of-the-art approaches for unsupervised person ReID. \* means applying a re-ranking method of k-reciprocal encoding [27]. Note that *Baseline* is built following [13] with ResNet-50 backbone and thus has nearly the same performance as *Theory* [13]. To save space, we only present the latest approaches in the main manuscripts and here we show comparisons with more approaches.

Unsupervised ReID	Venue		$I \rightarrow D$ Rank-1		$\rightarrow$ M Rank-1		$I \rightarrow C$ Rank-1		$\rightarrow C$ Rank-1		$\rightarrow$ M Rank-1		→D Rank-1
CAMEL [21]	ICCV'17			26.3	54.5								
PUL [3]	TOMM'18	_	_	20.3 20.5	$\frac{54.5}{45.5}$	_	-	_	_	_	_	-	_
PTGAN [18]	CVPR'18	_	27.4	20.5	45.5 38.6	_	_	_	_	_	31.5	_	17.6
SPGAN [2]	CVPR'18	22.3	41.1	22.8	51.5	_	_	_	_	19.0	42.8	_	17.0
TJ-AIDL [16]	CVPR'18	22.3	44.3	26.5	58.2	_	_	_	_	19.0	42.0	_	_
ARN [10]	CVPRW'18	$\frac{23.0}{33.4}$	44.3 60.2	20.5 39.4	70.3	_	_	_	_	_	_	-	_
MMFA [11]	BMVC'18	24.7	45.3	27.4	56.7	_	_	_	_	_	_	_	_
HHL [28]	ECCV'18	24.7	46.9	31.4	62.2	_	_	_	_	29.8	56.8	23.4	42.7
CFSM [1]	AAAI'19	27.3	49.8	28.3	61.2	_	_	_	_	20.0		20.4	-12.1
MAR [22]	CVPR'19	48.0	67.1	40.0	67.7	_	_	_	_	_	_	_	_
ECN [29]	CVPR'19	40.4	63.3	43.0	75.1	_	_	_	_	_	_	_	_
PAUL [20]	CVPR'19	53.2	72.0	40.1	68.5	_	_	_	_	_	_	_	_
SSG [4]	ICCV'19	53.4	73.0	58.3	80.0	_	_	_	_	_	_	_	_
PCB-R-PAST <sup>*</sup> [23]	ICCV'19	54.3	72.4	54.6	78.4	_	_	_	_	57.3	79.5	51.8	69.9
Theory [13]	PR'2020	48.4	67.0	52.0	74.1	46.4	47.0	28.8	28.5	51.2	71.4	32.2	49.4
ACT [19]	AAAI'20	54.5	72.4	60.6	80.5	48.9	49.5	30.0	30.6	64.1	81.2	35.4	52.8
Baseline	This work	48.4	67.1	52.1	74.3	46.2	47.0	28.8	28.4	51.2	71.4	32.0	49.4
Baseline + GDS	This work	52.9	71.4	57.1	78.5	48.0	48.9	30.7	32.5	63.6	81.6	44.1	64.0
Baseline + $GDS-H$	This work	55.1	73.1	61.2	81.1	49.7	50.2	34.6	36.0	66.1	84.2	45.3	64.9
B-SNR[7]	CVPR'20	54.3	72.4	66.1	82.2	47.6	47.5	31.5	33.5	62.4	80.6	45.7	66.7
B-SNR[7] B-SNR[7]+GDS	This work	54.3 57.2	72.4 74.6	68.6	82.2 84.9	47.6	47.5	31.5	33.5	$62.4 \\ 67.2$	80.6	45.7	69.9
B-SNR[7]+GDS-H	This work This work	59.7	76.7	72.5	89.3	49.8 50.7	<b>51.4</b>	38.9	<b>41.0</b>	68.3	86.7	51.0	71.5

mAP/Rank-1 for M $\rightarrow$ MSMT17 and D $\rightarrow$ MSMT17, respectively, which demonstrates the effectiveness of our proposed GDS constraint. SSG [4] also belongs to clustering-based approach. It exploits the potential similarity from the global body to local parts to build multiple clusters at different granularities. As a comparison, our *Baseline* and *Baseline+GDS-H* only consider the similarity at global body. Being simple in design, our final scheme *Baseline+GDS-H* outperforms the second best method SSG [4] by **2.7%** and **1.7%** in Rank-1 accuracy for M $\rightarrow$ MSMT17 and D $\rightarrow$ MSMT17, respectively.

In addition, to save space, we only present the latest approaches in the Section 4.6 "Comparison with State-of-the-Arts" in the main manuscripts and here we show comparisons with more approaches in Table 3.

# 6 More Visualization Results

Visualization of Dataset-wise (Global) Distance Distributions. To better understand how well our GDS constraint works, in Fig. 1, we not only visualize the dataset-wise Pos-distr and Neg-distr on the test set of target dataset (as shown in Fig. 6 in the main manuscripts), but also visualize the counterpart on the training set of target dataset. We have the following observations. 1) Thanks to the adaptation on the unlabeled target dataset and our GDS constraint, the distance distributions of our final scheme Baseline+GDS-H present a much better separability than that of other schemes. This trend can be observed on both the training set and test set. 2) On the training set, each scheme

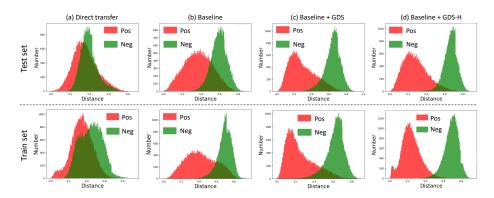


Fig. 1: Histograms of the distances of the positive sample pairs (red) and negative sample pairs (green) on the **test set (top)** and **train set (bottom)** of the target dataset Duke (Market1501 $\rightarrow$ Duke) for schemes of (a) *Direct transfer*, (b) *Baseline*, (c) *Baseline+GDS*, and (d) *Baseline+GDS-H*.

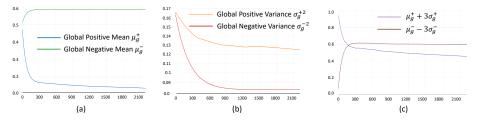


Fig. 2: Trend analysis of the learned dataset-wise (global) statistics in the training.

presents better separability than that on the test set, especially for our final scheme Baseline+GDS-H, which suggests that our GDS constraint is actually very helpful in promoting the separation after the optimization.

Trend Analysis of the Learned Dataset-wise (Global) Statistics. We observe the changing trend of the global statistics of distance distributions (including the mean  $\mu_g^+$  of global Pos-distr, the mean  $\mu_g^-$  of global Neg-distr, the variance  $\sigma_g^{-2}$  of global Neg-distr, the training process and show the curves in Fig. 2<sup>3</sup>. The horizontal axis denotes the identities of the epochs (30 iterations × 70 epochs = 2100 epochs). We observe that 1) as we expected, the centers/means of two distributions  $(\mu_g^+, \mu_g^-)$  and their hard tails  $(\mu_g^+ + 3\sigma_g^+, \mu_g^- - 3\sigma_g^-)$  become further apart as the training goes; 2) the two distributions variance  $(\sigma_g^{+2}, \sigma_g^{-2})$  become sharper since the variances become smaller as the training progresses.

 $<sup>^3</sup>$  We initialize the two distributions with mean of 0.5 and variance of 1/6 for the observation. Actually, we found the performance is not sensitive to the initialization values of the statistics.

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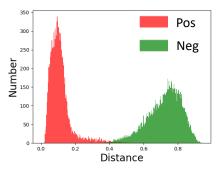


Fig. 3: Histograms of the distances of the positive sample pairs (red) and negative sample pairs (green) on the *training* set of the labeled dataset CUHK03 for fully supervised person ReID.

Table 4: Effectiveness of the proposed GDS loss and the distribution-based hardmining loss (H) for the fully supervised Person ReID.

	CUH	K03 (L)	MSMT17		
Supervised ReID	mAP	Rank-1	mAP	Rank-1	
Baseline	69.8	73.7	47.2	73.8	
$\operatorname{Baseline} + \mathbf{GDS}$	70.7	74.3	48.3	74.4	
$\operatorname{Baseline} + \mathbf{GDS}\text{-}\mathbf{H}$	71.4	75.5	<b>49.1</b>	74.9	

# 7 GDS Constraint Applied to Supervised Person ReID

We design the GDS constraint for addressing the inseparability of distance distributions in unsupervised person ReID, where there is no groudtruth labels for the target dataset. The use of either the pseudo labels or style transferred images results in noises and overlapping of the two distributions. For fully supervised person ReID, the proposed GDS is also expected to enhance the performance. However, on the benchmark datasets, due to the use of reliable labels and the over-fitting problem, we found the distance distributions on the training set are already well separated (see Fig. 3) and thus there left small optimization space for us. Quantitatively, as shown in Table 5, although our GDS brings some performance improvement (1.6% and 1.9% in mAP for CUHK03(L) and MSMT17, respectively), it is not significant in comparison with the unsupervised ReID setting.

# 8 Training Complexity Analysis

The increase of training time of our design in comparison with *Baseline* [13] is negligible. We build *Baseline* with the representative clustering-based method [13], and add the proposed GDS constraint in the training. Both our loss calculation and momentum update have very low computation complexity in compar-

	K-r	neans	DB	SCAN	HDBSCAN		
$M \rightarrow D$	mAP	Rank-1	mAP	Rank-1	mAP	Rank-1	
Baseline	40.2	57.9	48.4	67.1	49.6	67.9	
Baseline+GDS-H	49.0	67.2	55.1	73.1	55.7	73.6	

Table 5: Performance w.r.t different clustering algorithms for the  $M \rightarrow D$  setting.

ison with the convolutional operations of the network. Take the setting of using DukeMTMC-reID as source dataset and Market1501 as target dataset as an example, the training time of *Baseline* [13] and our scheme *Baseline+GDS-H* is 17.9 hours and 18.2 hours, respectively (*i.e.*, about 1.7% increase). The training time is comparable to that of the existing STOA methods (PAUL [20] with 16.3 hours, SSG [4] with 20.8 hours, MAR [22] with 25.6 hours). Note that all these training courses are conducted on a single 16G NVIDIA-P100 GPU.

## 9 Performance w.r.t Different Clustering Algorithms

The performance of the *Baseline* scheme with the cluttering approach of DB-SCAN is similar to that with hierarchical DBSCAN (HDBSCAN), 48.4% vs. 49.6% in mAP for  $M\rightarrow D$ , and both outperforms the *Baseline* scheme with K-means (40.2%). Our GDS constraint consistently brings improvement of 8.8%, 6.7%, and 6.1% for that with K-means, DBSCAN, and HBSCAN, respectively. For simplicity, we use DBSCAN by default in our experiments.

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