# Incorporating Reinforced Adversarial Learning in Autoregressive Image Generation

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**Abstract.** Autoregressive models recently achieved comparable results versus state-of-the-art Generative Adversarial Networks (GANs) with the help of Vector Quantized Variational AutoEncoders (VQ-VAE). However, autoregressive models have several limitations such as exposure bias and their training objective does not guarantee visual fidelity. To address these limitations, we propose to use Reinforced Adversarial Learning (RAL) based on policy gradient optimization for autoregressive models. By applying RAL, we enable a similar process for training and testing to address the exposure bias issue. In addition, visual fidelity has been further optimized with adversarial loss inspired by their strong counterparts: GANs. Due to the slow sampling speed of autoregressive models, we propose to use partial generation for faster training. RAL also empowers the collaboration between different modules of the VQ-VAE framework. To our best knowledge, the proposed method is first to enable adversarial learning in autoregressive models for image generation. Experiments on synthetic and real-world datasets show improvements over the MLE trained models. The proposed method improves both negative log-likelihood (NLL) and Fréchet Inception Distance (FID), which indicates improvements in terms of visual quality and diversity. The proposed method achieves state-of-the-art results on Celeba for  $64 \times 64$ image resolution, showing promise for large scale image generation.

**Keywords:** Autoregressive Models, Reinforcement Learning, Vector Quantized Variational AutoEncoders, Generative Adversarial Networks

### 1 Introduction

Image generation is a central problem in computer vision and has numerous applications. Nowadays, powerful image generation methods are mostly based on Generative Adversarial Networks (GANs), which was first introduced by Goodfellow *et al.* [19]. With the development of advanced network structures and large-scale training [11, 55], GANs are able to generate high-quality and high-resolution images. However, it is known that GANs do not capture the



Fig. 1: Sample comparison of the proposed reinforced adversarial learning with the MLE trained model on CelebA [30] and LSUN-bedroom [52] datasets. Results are randomly sampled.

complete diversity of the true distribution [7, 8]. Additionally, GANs are difficult to evaluate where hand-crafted metrics such as Inception Score [40] and Fréchet Inception Distance (FID) [22] must be used to test their performance.

Autoregressive models [33, 28, 34] directly optimize negative log-likelihood (NLL) on training data offer another way for image generation. These models are less likely to face the mode collapse issue due to their objective [38]. Additionally, the objective itself provides a good evaluation metric. PixelCNN [34] is a common choice due to its performance and computational efficiency. The introduction of two recent works [38, 16], which make use of PixelCNNs, vector quantization [32] and hierarchical-structure have shown comparable results vs. GANs. These advancements could open up a new avenue for image generation research.

On the other hand, there are several open problems in likelihood-based methods. As pointed out in [47], optimizing NLL does not necessarily lead to generating realistic images as this objective is not a good measure of visual quality. Another issue is the exposure bias. The sampling of PixelCNN is sequential, which is a different procedure from its training stage. This discrepancy can be troublesome as small errors during the sampling can accumulate towards the next steps, which may lead to unrealistic samples [9]. To alleviate these issues, VQ-VAE-2 [38] proposed to use the classifier based rejection sampling. This technique can eliminate low-quality samples based on an ImageNet pre-trained classifier. Classifier based rejection sampling helps VQ-VAE-2 achieve competitive results versus BigGAN [11]. Nevertheless, this method is time exhaustive, especially considering the slow sampling speed of autoregressive models. Additionally, class information might not be always available in most datasets.

In this paper, we aim to leverage both advantages of GANs and likelihood models. Consequently, our objective is to further improve the visual fidelity of autoregressive models while addressing the exposure bias issue. We focus on the VQ-VAE framework [32,38], which relies upon PixelCNN [34] for latent code generation and uses a pre-trained decoder to reconstruct images. However, PixelCNN [34] generates sequences of discrete codes. Therefore, we cannot directly optimize it directly with GAN objectives. To fix this issue, we regard the sampling process of PixelCNN as a sequential decision-making process and optimize it by Reinforced Adversarial Learning (RAL). A discriminator network is trained to distinguish between real & fake images and provides rewards to the PixelCNN. We compare our proposed method on two image generation benchmarks to demonstrate that RAL can indeed improve both FID and NLL significantly.

Adversarial training for sequence generation with RL is first explored in SeqGAN [54] but there is a lot of room for improvement, especially for images. Compared to text or music generation tasks studied in SeqGAN, image generation is more complex due to longer sequences and strong spatial correlation of images. In this paper, in addition to applying RAL work for image generation for the first time, we also propose a partial generation idea to address the issue with long-sequences. Moreover, we include a method that enables the use of intermediate rewards for spatial correlation. The proposed method also enables the incorporation of independently trained modules in VQ-VAE. Our experiments show that RAL can greatly improve one of the most successful image generation methods for autoregressive models, which has a lot of potential for future work.

In summary, our contributions are four-fold:

- We propose to augment the autoregressive image generation with adversarial training by using reinforcement learning to further improve the image quality while incorporating collaboration between independently trained modules.
- We utilize a patch-based discriminator to enable intermediate rewards.
- We propose partial generation for faster training to addresses the sampling issue of long sequences.
- We conduct extensive experiments to show that the proposed method significantly improves over the MLE trained baselines in different settings for both synthetic and real datasets.

The rest of the paper is organized as follows. In Sect. 2, we briefly introduce related works. In Sect. 3, we introduce the basics of VQ-VAE & VQ-VAE-2 and we describe our method in detail in Sect. 4. Implementation details are provided in Sect. 5.1, experimental results are presented in Sect. 5 and finally, we conclude the paper in Sect. 6.

#### 2 Related Work

# 2.1 Generative Models

GANs [19] and conditional-GANs [31] have shown a huge success for many problems in computer vision [13, 2, 4, 3, 51, 5, 21, 1] and speech processing [39,

43, 41, 44, 42, 56]. Advanced architectures such as SaGAN [55], StyleGAN [26] and BigGAN [11] have shown GANs' superiority in terms of image quality compared to Variational Autoencoder (VAE) [28] and autoregressive models, e.g., PixelCNN [34]. Additionally, GANs are much faster in inference compared to autoregressive models. However, it is known that GANs models can not fully capture the data distribution and may sometimes suddenly drop modes [7, 8]. Moreover, there are no perfect metrics to evaluate the sampling quality of GANs.

Autoregressive models are less likely to face the mode collapse and can be easily evaluated by measuring log-likelihood [38]. However, these models are expensive to train and extremely slow at the sampling time when trained in the pixel space. Performing vector quantization [32, 14, 48] and training a PixelCNN prior in discrete latent space is much more efficient than pixel space, which enables the scaling to large resolution images. Following this idea, the recently introduced VQ-VAE-2 framework managed to achieve competitive results compared to state-of-the-art GANs. Concurrently with VQ-VAE-2, Fauw et al. [16] followed a similar approach to combine autoencoders with autoregressive decoders. The advantage of VQ-VAE-2 is the feed-forward design of the decoder, making it faster for sampling. Due to faster sampling time, VQ-VAE-2 is more feasible for our work, which requires sampling of numerous images during the training.

Although these aforementioned autoregressive models achieve decent improvements in terms of image coherence and fidelity than before [34, 12], GANs are still preferred due to sampling speed and image quality. Additionally, as mentioned by Theis et. al [47], good performance on log-likelihood training objective does not always guarantee good samples. In order to reduce this gap, VQ-VAE-2 proposes to use classifier-based rejection sampling to trade-off diversity and quality inspired by BigGAN [11]. However, this approach requires the autoregressive prior to sample many latent codes, which is time exhaustive and not ideal for real-world problems. Additionally, the rejection sampling method relies on a ImageNet pretrained classifier and might not be available for another dataset such as CelebA [30] and LSUN-bedroom [52]. Lastly, the rejection sampling method decreases diversity in image samples. We propose to use reinforcement learning to improve the sampling quality of autoregressive models and enable a similar mechanism for training and testing.

## 2.2 Reinforcement Learning in Sequence Generation

RL for sequence generation has been applied by [37], which uses bilingual evaluation understudy (BLEU) [35] as a reward function to guide the generation process. SeqGAN [54] is the first to train a discriminator through adversarial learning and use reinforcement learning based on policy gradient [46] to provide rewards for seq-to-seq network [45]. Recent works [18, 23] also showed that adversarial training can be used to iteratively update images where rewards are estimated by a discriminator network. In this work, we similarly employ a discriminator network to provide rewards for the generated samples and improve sampling quality. We enable intermediate rewards by using a PatchGAN [24] network and use a partial generation procedure to handle long sequences.

# 3 Background: VQ-VAE & VQ-VAE-2

Our method is built upon VQ-VAE [32] & VQ-VAE-2 [38] frameworks that are trained in two stages as follows:

Stage 1: Learning Hierarchical Latent Codes. In this stage, VQ-VAE learns an encoder E that transforms an image into a set of features, a codebook C that maps the real-valued features into a set of discrete latent codes and a decoder U that reconstructs the image from these latent codes. E, C and U are learned together as in [32]. However, the reconstruction in VQ-VAE is not perfect due to the quantization, therefore VQ-VAE-2 [38] proposed to learn hierarchical latent codes to alleviate this problem. In VQ-VAE-2, the first hierarchy called top-level latent codes captures global image information such as shape and structures while the other hierarchy called bottom-level latent captures fine-grained details. Once stage 1 is learned, an input image can be represented as the hierarchical latent codes for compression and reconstructed by the decoder.

Stage 2: Learning Priors Over Latent Codes. PixelCNN [34] is an autoregressive model and has been previously applied to learn image distributions in the pixel space. In VQ-VAE, PixelCNN is used to learn priors in the latent space, which has much smaller dimensionality than the pixel space. For the two hierarchies in VQ-VAE-2, PixelSNAIL [12] is used to learn the top-level latent codes while a lighter PixelCNN is used to learn the bottom-level as the size of the bottom-level latent codes is larger. These two models are trained separately by MLE. After the training, latent codes sampled from the PixelCNN priors can be reconstructed with the pretrained decoder to an image.

## 4 Reinforced Adversarial Learning

There are several drawbacks of PixelCNNs priors used in the VQ-VAE frameworks [32, 38]. First, they are trained with MLE which is not a good measure of sampling quality [47]. Second, during the training, all latent codes are estimated from the real images while during inference each code is sampled, which could never be observed during the MLE training. Such discrepancy could result in an unrealistic generation. Lastly, each hierarchy and the decoder in the VQ-VAE-2 framework are trained separately, which may not collaborate well when put together for sampling images.

In this section, we describe how we introduce adversarial learning from GANs into likelihood models to leverage the best from both worlds. Our motivation is to let the PixelCNNs be able to generate samples that can fool the discriminator that is trained to distinguish between real and fake images. In this way, our PixelCNNs are trained to generate realistic sequences and the training process is exactly the same as inference. In addition, the harmony of different PixelCNNs and the decoder are also improved since they are optimized together. One issue is that PixelCNN cannot be directly optimized by the adversarial loss, which we solve by employing reinforcement learning. Parameters of Encoder & Decoder are fixed since including them to the training corrupts the image decoding procedure, which results in having poor quality of images even when using real latent maps.

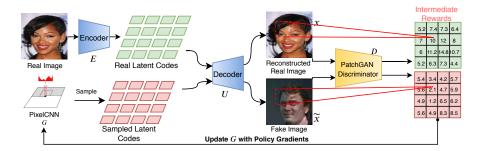


Fig. 2: Overview of the proposed Reinforced Adversarial Learning (RAL) framework. Initially, PixelCNN G is used to sample fake latent codes which are then fed into Decoder to reconstruct the fake image. Similarly, the real image can be reconstructed from the real latent codes. We use PatchGAN Discriminator to provide rewards for overlapping regions in the image. These rewards can then be used to update G with policy gradients.

We illustrate our solution in Sect. 4.1. Our patch-based discriminator and reward definition are presented in Sect. 4.2. We describe the idea of partial generation that is useful for the generation of large images in Sect. 4.3. Training details are given in Sect. 4.4. An overview of the proposed RAL framework is shown in Figure 2.

#### 4.1 Policy Gradients

For simplicity, let us first consider learning a single PixelCNN G on one hierarchy of latent codes. The extension to multiple PixelCNNs on multiple hierarchies (VQ-VAE-2) is straightforward.

In adversarial training, a generator is directly optimized to maximally confuse a discriminator. However, at each time  $t \in [0, T-1]$ , our PixelCNN generates a discrete code  $c_t$  based on the conditional probability  $G(c_t|c_0,...,c_{t-1})$  given all the previous codes  $(c_0,...,c_{t-1})$ . This process is non-differentiable and thus cannot be directly optimized. However it can be regarded as a decision making process where the state  $s_t = (c_0,...,c_{t-1})$  and the action  $a_t = c_t$ . We use policy gradients [46] to solve this problem where the objective is:

$$J_G = \mathbf{E}_{a \sim G}[R_T] \tag{1}$$

where  $R_T$  is the reward for the whole sequence of latent codes generated by G. The gradients of Equation 1 can be defined as:

$$\nabla_{\theta} J_G \propto \mathbf{E}_{a_t \sim G} \left[ \nabla_{\theta} \log G(a_t | s_t) Q(s_t, a_t) \right] \tag{2}$$

where  $\theta$  is the parameters of the PixelCNN.  $Q(s_t, a_t)$  is the action-state value and is defined as:

$$Q(s_t, a_t) = \sum_{k=t+1}^{T} \gamma^{k-t-1} r_k$$
 (3)

where  $r_k$  is the reward at time step k, which can be obtained by the discriminator and will be discussed later.  $\gamma$  is the discounted factor within the range of [0, 1].

We use the REINFORCE [50] algorithm to roll-out the whole sequence after  $a_t$  is sampled by using the same PixelCNN G. In our experiment, we only do one Monte-Carlo roll-out for the training-speed concern. Finally, G can be updated as follows where the  $\alpha$  is learning rate:

$$\theta \leftarrow \theta + \alpha \nabla_{\theta} J_G \tag{4}$$

#### 4.2 Discriminator

After a sequence of latent codes  $(c_0, ..., c_{T-1})$  is generated, the decoder U is used to reconstruct the image  $\tilde{\mathbf{x}}$ , as shown in Figure 2. Then a discriminator D is trained to distinguish between the generated and real images (real images are also their reconstructed version). We use the WGAN loss [6, 20] instead of the original GAN loss proposed in [19]. Since it provides smoother gradients which enable the generator to still learn even when the discriminator is performing strong. The loss function of our discriminator is defined as:

$$L_D = -\mathbf{E}_{\mathbf{x} \sim p_d}[D(\mathbf{x})] + \mathbf{E}_{\tilde{\mathbf{x}} \sim G}[D(\tilde{\mathbf{x}})] + \lambda_{gp} \mathbf{E}_{\hat{\mathbf{x}}}[(||\nabla_{\hat{\mathbf{x}}} D(\hat{\mathbf{x}}))||_2 - 1)^2]$$
(5)

where  $p_d$  is the distribution of real images. The final term is the gradient penalty weighted by  $\lambda_{gp}$ .  $\hat{\mathbf{x}}$  is an image sampled uniformly along a straight line between real and generated images.

Our discriminator follows a similar structure to the PatchGAN discriminator [24]. In contrast to traditional GAN discriminators that only produce a single scalar output, the PatchGAN discriminator can provide a score map S, each element of which corresponds to the score of a local image patch as shown in Figure 2. There are several advantages of using this type of discriminator. First, it provides a good measure of the realism of local patches. Second, the scores can be used as intermediate rewards which can alleviate the issue of sparse rewards in RL training. Third, its fully convolutional structure can handle arbitrary image sizes, which is convenient for our partial generation.

The intermediate reward at every time step can be computed by upsampling the score map S to the original size of the latent codemap as shown in Figure 2. The reward  $r_{t+1}$  of the sampled code  $c_t$  has a corresponding location at the upsampled score map and can be easily obtained. Since each code is contained in a local region, the action-state value function  $Q(s_t, a_t)$  thus more focus on the local realism.

Our *single reward* function is defined as:

$$r_{t} = \begin{cases} 0, & t < T \\ D(\tilde{\mathbf{x}}), & t = T \end{cases}$$
 (6)

where  $D(\tilde{\mathbf{x}})$  is the average value of the score map S. In this case the action-state value function  $Q(s_t, a_t)$  focus more on the long-term reward, i.e. the realism of the whole image.

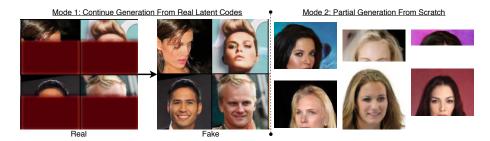


Fig. 3: Examples for partial generation from G. The proposed idea, improves the training speed of RL algorithm.

#### 4.3 Partial Generation

In order to generate large-size images, the length of sampled latent codes also needs to be increased, which is time-exhaustive. This is especially troublesome as our RL training requires many Monte-Carlo roll-outs at each iteration. As a solution, we propose to use partial generation whose central idea is to only sample partial images, which can already provide meaningful rewards while improving sampling efficiency greatly.

Specifically, the partial generation works under two modes: (1) continue generation from real latent codes and (2) partial generation from scratch. During each roll-out in RL training, the algorithm first randomly decides one mode. If mode-1 is selected, then a random number representing the number of rows of real latent codes is chosen. Then following these real codes, G samples the rest of the sequence. If mode-2 is selected, a random number representing the number of rows of fake latent codes is chosen. Then G samples this number of codes from scratch. The two modes are essential and improve the generation of the PixelCNN on different image regions. In addition, mode-1 provides real latent codes as context and is useful for the image completion task. Figure 3 shows some sampled examples of both the two modes. It should be noted that although the sampled codes correspond to different image sizes, as our discriminator is fully convolutional and thus has no issue.

#### 4.4 Training

VQ-VAE is first trained with the two stages as described in Sect. 3 and PixelCNN is pretrained with the MLE objective. Then our RL training starts. We use Adam optimizer [27] with  $\beta_1 = 0.5$ ,  $\beta_2 = 0.999$  and set the learning rate of the discriminator and PixelCNN to 1e-4, 4e-6 respectively with the mini-batch size of 16. Initially, the discriminator is trained for 100 iterations to catch up with the pretrained PixelCNN. During the RL training, for each PixelCNN update, the discriminator is updated 5 times and updates are performed iteratively. When there are two hierarchies of latent codes available, both the PixelCNN models are trained at the same time which encourages collaboration between them. Outputs

from the discriminator are first normalized to the range of (-1, 1) before updating the PixelCNNs. The normalization is performed with respect to the highest value from a set of fake and real images. Without normalizing the discriminator's outputs, rewards become unreliable as, after each update, the discriminator's outputs may change drastically even with the WGAN penalty. By normalizing rewards based on the maximum value of real and fake images, rewards act as an evaluation score from the current state of D. For the partial generation, the algorithm randomly switches between different modes and samples a random number of rows. We set  $\lambda_{gp}$  in Eq. 5 to 10 and the discounted factor  $\gamma$  to 0.99.

# 5 Experiments

We first conduct experiments on a synthetic dataset similarly to [54,49] in Sect. 5.2. The synthetic dataset is constructed from a pre-trained PixelCNN [34] prior, which we denote as the oracle model  $G_{\rm oracle}$ . The oracle model is used to provide the true data distribution and the generator is trained to fit the oracle distribution. The advantage of having an oracle model is that the generated samples can be evaluated with NLL which is not possible for real data.

Our second experiment in Sect. 5.3 is for real-world images where we train our models in the CelebA dataset [30] with different scales:  $64 \times 64$ ,  $128 \times 128$  and  $256 \times 256$ , in addition to the LSUN-bedroom [52]. As an evaluation metric, we use Fréchet Inception Distance (FID) [22], which uses an Inception network to extract features to compare the closeness of real and fake images statistics. Lower FID means better image quality and diversity. Several experiments with different settings and architecture details are included in the supplementary material.

We also perform an ablation study in Sect. 5.4 followed up by a use-case of the proposed method for image completion task in Sect. 5.5, which also demonstrates the proposed method captures global structure better than MLE trained model as the generated sequences are more correlated with the real ones.

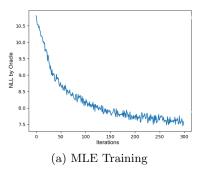
#### 5.1 Implementation Details

This section describes the implementation details of different modules used in RAL. The detailed information on architecture choices is included in our supplementary material.

**Encoder.** VQ-VAE [32] encoder is used to compress images to latent space. Each layer includes a transposed convolution for downsampling. For hierarchical codes, two latent levels are used i.e., top and bottom. Images are encoded into following latents codes for different resolutions: a)  $64 \times 64 \rightarrow 8 \times 8$ , b)  $128 \times 128 \rightarrow 16 \times 16$ ,  $32 \times 32$ , c)  $256 \times 256 \rightarrow 32 \times 32$ ,  $64 \times 64$ .

**Decoder.** VQ-VAE decoder is used to reconstruct images from latent codes. For hierarchical codes, the bottom-level code is conditioned on the top level. The network consists of transposed convolutional layers for upsampling.

**PixelCNN/PixelSNAIL.** Similar to VQ-VAE-2, we use PixelCNN with self-attention layers to model top-priors. For bottom-priors, which is more computationally expensive, we remove self-attention layers and reduce the number of



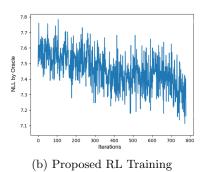


Fig. 4: Negative log-likelihood during the training iterations.

residual channels. To improve the sampling speed from prior networks, we use caching similar to [36] and avoid redundant computation. Note that, we use a smaller VQ-VAE-2 architecture compared to [38] due to computational limitations. The main issue is the model capacity requirement for MLE pre-training. Even with  $8\times V100$  GPUs (8x16GB), which is the best machine we can get, we were barely able to use similar networks designed in the VQ-VAE-2 for  $128\times128$ , but not enough for  $256\times256$  due to the increase in latent code sizes.

**PatchGAN Discriminator.** The discriminator has a similar convolutional architecture to the encoder network, while at the patch level to classify whether a patch is real or fake. The discriminator has 5 strided convolutions which output a  $4\times 4$  reward map from a  $128\times 128$  image. We also experiment with different output scales in our ablation study to find the optimum architecture.

#### 5.2 Synthetic Experiments

We first perform synthetic experiments on the CelebA dataset with the image resolution of  $64 \times 64$ , which are mapped into one level of  $8 \times 8$  latent codes by the encoder. Instead of directly training on real images, we first train a PixelCNN  $G_{\rm oracle}$  on the  $8 \times 8$  latent codes. Then this model is used as an oracle data generator to provide training data. The advantage is that we can have accurate NLL estimation, which cannot be achieved with real images since the oracle generator for real images is unknown.

Next, a lighter PixelCNN<sup>3</sup>  $G_{\rm MLE}$  is trained on training samples generated by  $G_{\rm oracle}$  with the MLE objective, which is the VQ-VAE baseline. Our method fine tunes  $G_{\rm MLE}$  with our RL training to estimate another model  $G_{\rm RL}$ . For this experiment we do not use partial generation since the size of latent codes is already small. The ground truth NLL estimation of a generator G can be computed as:

 $<sup>^3</sup>$  We use a lighter PixelCNN so that the MLE model cannot be easily trained towards the oracle model.

Table 1: NLL and FID values for Oracle Experiments.

Table 2: FID values for real-world experiments. The number in parenthesis is FID on reconstructed real images.

Dataset	CelebA	CelebA	CelebA	LSUN-bedroom
Dataset	$64 \times 64$	$128 \times 128$	$256 \times 256$	$128 \times 128$
MLE	5.35	58.07 (21.28)	69.37 (55.11)	47.77 (23.14)
Single Reward	3.24	49.24 (16.49)	66.44 (53.54)	39.86 (19.37)
Intermediate Reward	4.10	$51.91\ (19.68)$	$64.72 \ (51.38)$	$36.47\ (16.06)$
PGGAN [25]	-	7.30	-	$8.34 - 256 \times 256$
COCO-GAN [29]	4.00	5.74	-	$5.99 - 256 \times 256$

$$NLL_{oracle} = -\mathbb{E}_{c_t \sim G} \left[ \sum_{t=0}^{T-1} \log G_{oracle} \left( c_t | c_{0:t-1} \right) \right]$$
 (7)

We report the NLL results in Table 1 and the learning curves in Figure 4. It can be seen that our RAL with different rewards improve the MLE-trained model even though our objective is not NLL. In Table 1, we also show that our methods get better FID scores when compared with both fake images produced by  $G_{\rm oracle}$  and real images.

#### 5.3 Real World Experiments

Given the success of oracle experiments, we further evaluate our method for real-word image generation and report the FID values [22] in Table 2. Note that the FID scores outside/inside parenthesis are computed between generated images and the real images/reconstructed real images. The large FID scores on  $128 \times 128$  images are mainly caused by the lossy compression of the VQ-VAE encoder-decoder, which is also mentioned by [38]. In addition, only reconstructed real images are used during our training. Therefore the scores inside the parenthesis are more meaningful for comparison.

Results show that our models improve the MLE trained model in all settings by a large margin. In addition, our single-reward model achieves the best FID score on CelebA  $64 \times 64$  resolution even when compared to the state-of-the-art GAN models [25, 29] (the compression loss is relatively small on  $64 \times 64$  resolution and thus our FID score is not affected much). For  $128 \times 128$  resolution, the use of intermediate reward performs better on the LSUN-bedroom while the single reward is better for CelebA. We use a much smaller architecture than the one reported in [38] for CelebA  $256 \times 256$  experiments. The proposed RAL still



Fig. 5: Image samples on CelebA dataset with  $128 \times 128$  resolution. The ratio of good samples from MLE model is less than ours.

Table 3: Ablation experiments on CelebA with  $128 \times 128$  resolution. The number in parenthesis is FID score on reconstructed real images.

(a)		(b)		
(a)			FID	
	FID	Single reward, D output: $8 \times 8$	53.15 (18.28)	
Partial-Gen. (Propos	ed) <b>49.24</b> ( <b>16.54</b> )	Single reward, D output: $4 \times 4$	49.24 (16.54)	
Full-Gen.	51.91 (20.25)	Single reward, D output: $2 \times 2$	49.78 (17.68)	
RAL on Top	54.82 (19.20)	Interm. reward, D output: $8 \times 8$	50.22 (18.65)	
RAL on Bottom	55.02 (19.80)	Interm. reward, D output: $4 \times 4$	54.835 (19.47)	
		Interm. reward, D output: $2 \times 2$	55.37 (20.99)	

improves the MLE trained model which demonstrates the effectiveness of the proposed method for larger latent codes.

We provide qualitative visual comparisons with the MLE trained model for the Celeba dataset in Figure 5 as well as LSUN-bedroom dataset in Figure 6. As can be seen, the main problem of the MLE trained model is that it generates visually good and bad images from the same model. This is mostly due to accumulating errors during the sampling and mismatch of training/testing procedures. Also, note that we do not use any classifier-based rejection sampling proposed in [38]. However, as the MLE trained models is additionally optimized via GAN loss, better-quality samples are produced.

#### 5.4 Ablation Study

In Table 3, we investigate different modules of the proposed method using the CelebA dataset with the image resolution of  $128 \times 128$ . In Table 3(a), the use of partial generation outperforms the full-generation. Note that both configurations are trained for the same time interval for a fair comparison. For all settings in



Fig. 6: Image samples on LSUN-bedroom dataset with  $128 \times 128$  resolution. The ratio of good samples from MLE model is less than ours.

Table 3 (a), we used single-reward, estimated from a discriminator, which outputs a  $4 \times 4$  output. In Table 3(a), we also test the effect of applying RAL on top and bottom priors independently, which achieves worse FID than the proposed joint training. This presents that the proposed RAL indeed enhances the collaboration of independently MLE trained priors.

Secondly, we test single and intermediate reward configurations with different score outputs from the discriminator in Table 3(b). The score map is adjusted by changing the number of convolutional layers. The single reward works best with the score map of  $4 \times 4$ . Intermediate reward works best with an  $8 \times 8$  score map. We also tried using larger score map outputs but did not observe improvements.

## 5.5 Image Completion

Image completion/inpainting [10, 15] is a process of restoring missing/damaged parts of the image. As the generation of autoregressive models is sequential, i.e., the generation of the current pixel is conditioned on the previous pixels, autoregressive models can be used for image completion. As in most image generation problems, GANs are top-performing models for this task [17, 53] but we believe this is a good application for comparisons with the MLE model.

In Figure 7, we perform some qualitative results with the LSUN-bedroom  $(128 \times 128)$  dataset with different image completion settings. Firstly, a number of rows of input images (first row) are hidden (second). These hidden rows can be simply eliminated by zeroing out their corresponding locations in latent maps. Next, autoregressive models can continue sampling the remaining codes where completed reconstructed images are shown in the last three rows. We illustrate two modes of the proposed model to show the proposed method can generate diverse samples.



Fig. 7: Image completion experiment for the MLE trained method versus the proposed method. Images in the first row are hidden with masking function in the second. The generation shown in rows 3, 4 and 5 continue from visible regions of the image and the corresponding location can be approximated by the encoder.

In the first column, a glimpse of a room is given where both methods successfully include the window in the generated image. The proposed method tends to produce more realistic samples due to its adversarial learning. Another interesting example can be seen in the final column, where the proposed method can reproduce the remaining regions more realistically compared to the MLE trained model.

# 6 Conclusion

Our proposed idea has several advantages compared to traditional autoregressive models. By utilizing reinforcement learning, we bridge the gap between training and testing procedures while enabling the autoregressive model to take advantage of GAN training. Additionally, we use partial generation to improve the training and use two different image rewards. Last but not least, we show that the proposed method can improve the collaboration of independently trained hierarchical modules. To our best knowledge, our framework is first to enable the adversarial learning in PixelCNNs and does not solely depend on the traditional objective function of autoregressive models for good sample quality. A possible future direction would be to extend the proposed framework to higher resolution images which would be possible with faster sampling times.

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