Data Invariants to Understand Unsupervised Out-of-Distribution Detection Supplementary Material

Lars Doorenbos[®], Raphael Sznitman[®], and Pablo Márquez-Neila[®]

University of Bern, Bern, Switzerland {lars.doorenbos,raphael.sznitman,pablo.marquez}@unibe.ch

1 Supplementary Material

1.1 Dataset Details

We briefly describe all datasets used in our experiments. An overview of our experimental set-up is given in Table S1.

- CIFAR10 [28]. (In) Small, natural images divided into 10 classes. For uniclass, one class forms the in-distribution, with its test set used in the evaluation. For shift-low-res, all 50000 training images are used for training when considered in-distribution, and all 10000 test images are used for testing. (Out) The remaining 9 classes are used as OOD for uni-class, subsampled to 1000 images.
- **CIFAR100** [28]. (In) 20 experiments with the training set of one of the semantic superclasses as the in-distribution, with its test set used during evaluation. (Out) Images from the remaining superclasses, subsampled to 500 images.
- MVTec [4]. (In) Between 60 and 391 aligned images of 15 different objects and textures. 12-60 images are used as the in-distribution at test time. (Out) 30-141 images of defect objects are used as OOD.
- **OCT.** (In) A collection of 58849 retinal Optical Coherence Tomography images used for training, and 300 for testing. (Out) Corrupted OCT scans built as described in [31].
- **Chest** [59]. (In) The NIH Clinical Center ChestX-ray dataset containing 85524 training images. We use 300 images from the test set during evaluation. (Out) Corrupted X-ray scans as described in [31].
- NIH [55]. (In) A collection of 4261 healthy X-ray scans of the NIH Clinical Center ChestX-ray dataset. The healthy test scans are used as the in-distribution during evaluation. (Out) Pathological scans from the same dataset.
- DRD [17]. (In) 25809 healthy high-resolution retinal fundus photographs. Healthy test scans are again used during evaluation.(Out) Retinal fundus photographs depicting 4 different levels of diabetic retinopathy (DR). The level of DR is indicated by a digit next to the
- method's name (DRD1–DRD4). SVHN [35]. A dataset consisting of images of house numbers. We only use it as an OOD dataset, where the test set is reduced to 10000 samples.

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- **DomainNet** [37]. (In) The train and test images from the first 173 classes are used for training and evaluation respectively (as in [23]). We perform 10 experiments with the real images, and 10 with infographs. (Out) 10 domainclass combinations are used as OOD datasets. We avoid using Real-B and Infograph-B as OOD in the first and the second group of experiments respectively. All test sets are downsampled to 5000 images.

Category	# Tasks	Tasks	# train	# in	# out
	10	{airplane,automobile,bird,cat,deer, dog frog horse ship truck} rest.	5000	1000	1000
uni-class	20	2500	500	500	
uni-ano	15	{bottle,cable,capsule,carpet,grid,hazelnut, leather,metal nut,pill,screw,tile, toothbrush,transistor,wood,zipper}:defect	60-391	12-60	30-141
	1	OCT:corruptions	58849	300	300
uni med	1	Chest:corruptions	85524	300	300
um-meu	1	NIH:pathology	4261	677	667
	4	DRD:DRD1-4	25809	500	500
shift-low-res	1	CIFAR10:SVHN	50000	10000	10000
	10	Real A:{Quickdraw A,Quickdraw B,Infograph A, Infograph B,Sketch A,Sketch B, Clipart A,Clipart B,Painting A,Painting B}	61817	5000	5000
shift-high-res	10	Infograph A:{Quickdraw A,Quickdraw B, Sketch A,Sketch B,Real A,Real B, Clipart A,Clipart B,Painting A,Painting B}	14069	5000	5000

Table S1: Experimental set-up.

1.2 Implementation Details

We provide a short description of all models compared and their implementations. All modes make use of a ResNet-101 and rescale input images to 224×224 unless stated otherwise.

- **Glow** [26] is a generative flow-based model, that allows for the exact computation of the likelihood, which we use as the anomaly score at test time. We use the implementation of ¹, and an architecture with three blocks of 32 layers each. Images are resized to 32×32 .
- IC [51] aims to correct the high likelihood that generative models tend to assign to simple inputs, such as constant color images. To this end, IC computes the ratio between the likelihood of the generative model and a complexity

¹ https://github.com/y0ast/Glow-PyTorch

score of the input image. We used the Glow described above as our generative model and the length of the PNG image encoding as the complexity estimate.

- HierAD [47] computes the ratio between the Glow generative model likelihood and a general background likelihood consisting of a Glow model trained on the 80 Million Tiny Images dataset [56], provided at ². To make the method fully unsupervised, we do not use their proposed outlier loss during training.
- MHRot [20] trains a multi-headed classifier to predict the correct transformation applied to an image. At test time, the classifier's softmax scores are combined for a final OOD score. Models are trained with the default settings until convergence of the validation loss.
- **DDV** [31] aims to build an efficient latent representation by iteratively maximizing the log-likelihood of the low-dimensional latent vectors of the training images. Anomaly scores are given by the negative log-likelihood. We use our own implementation of DDV, following the settings described in its paper, i.e., a latent space of dimensionality 16 and a bandwidth of 10^{-2} [31].
- **MSCL** [40] uses a novel contrastive loss function to fine-tune the final two blocks of a pretrained network, and combines this with an angular center loss for a final score. We used the official implementation with the learning rate set to $5 \cdot 10^{-5}$, as described in the paper, and trained until convergence.
- **CFlow** [18] fits a normalizing flow network to features extracted from a pretrained network at multiple scales, conditioned on spatial information from a positional encoder. Anomaly scores are computed by aggregating the multiscale likelihoods, upsampled to the original resolution. We again use the default hyperparameters.
- **DN2** [2] scores outliers by computing the mean distance to its 2 nearest neighbour on features extracted from the penultimate layer of a network pretrained on ImageNet.
- **SSD** [50] uses contrastive learning for self-supervised representation learning. Then, it scores samples by the Mahalanobis distance computed at the last layer. All images were resized to 32×32 . We use the default settings described in the official implementation.
- **MahaAD** [41] is the Mahalanobis anomaly detector. Besides the ResNet-101, we also show results with an EfficientNet-b4 as described in [41]. With the ResNets, we resize images to 224×224 , while for the EfficientNet-b4 this is 380×380 .

1.3 Extended results

In Table S2 to Table S8 we dissect the per-task results from Table 1, reporting the AUC scores for each individual experiment and including some additional methods that were omitted from the main text for clarity.

 $^{^2}$ https://github.com/boschresearch/hierarchical_anomaly_detection

Table S2: AUC scores for CIFAR10 experiments of *uni-class*. First published (FP) column contains the dates of first online appearance. * Our results

	Airplane	Automobile	Bird	Cat	Deer	Dog	Frog	Horse	Ship	Truck	Average	FP
OCSVM [49]	63.0	44.0	64.9	48.7	73.5	50.0	72.5	53.3	64.9	50.8	58.5	Dec 1999
AnoGAN [48]	67.1	54.7	52.9	54.5	65.1	60.3	58.5	62.5	75.8	66.5	61.8	${\rm Mar}~2017$
RCAE [8]	72.0	63.1	71.7	60.6	72.8	64.0	64.9	63.6	74.7	74.5	68.2	Feb 2018
GT [15]	74.7	95.7	78.1	72.4	87.8	87.8	83.4	95.5	93.3	91.3	86.0	May 2018
Glow* [26]	76.1	44.5	60.3	57.3	43.9	55.1	36.2	46.4	71.0	46.4	53.7	Jul 2018
LSA [1]	73.5	58.0	69.0	54.2	76.1	54.6	75.1	53.5	71.7	54.8	64.1	Jul 2018
DSVDD [42]	61.7	65.9	50.8	59.1	60.9	65.7	67.7	67.3	75.9	73.1	64.8	Jul 2018
IIC [25]	68.4	89.4	49.8	65.3	60.5	59.1	49.3	74.8	81.8	75.7	67.4	Jul 2018
DIM [21]	72.6	52.3	60.5	53.9	66.7	51.0	62.7	59.2	52.8	47.6	57.9	${\rm Aug}~2018$
OCGAN [38]	75.7	53.1	64.0	62.0	72.3	62.0	72.3	57.5	82.0	55.4	65.6	${\rm Mar}~2019$
MHRot [20]	77.5	96.9	87.3	80.9	92.7	90.2	90.9	96.5	95.2	93.3	90.1	Jun 2019
CapsNet [29]	62.2	45.5	67.1	67.5	68.3	63.5	72.7	67.3	71.0	46.6	61.2	Jul 2019
IC* [51]	38.3	62.0	45.5	61.5	48.7	63.9	62.6	63.7	48.4	58.8	55.3	Jul 2019
E3Outlier [58]	79.4	95.3	75.4	73.9	84.1	87.9	85.0	93.4	92.3	89.7	85.6	Sep 2019
DDV* [31]	83.2	58.5	55.4	56.9	61.2	57.9	63.3	57.5	88	71.2	65.3	Oct 2019
DeepIF [36]	-	-	-	-	-	-	-	-	-	-	88.2	Oct 2019
CAVGA-DU [57]	65.3	78.4	76.1	74.7	77.5	55.2	81.3	74.5	80.1	74.1	73.7	Nov 2019
U-Std [5]	78.9	84.9	73.4	74.8	85.1	79.3	89.2	83.0	86.2	84.8	82.0	Nov 2019
InvAE [24]	78.5	89.8	86.1	77.4	90.5	84.5	89.2	92.9	92.0	85.5	86.6	Nov 2019
DROCC [16]	81.7	76.7	66.7	67.1	73.6	74.4	74.4	71.4	80.0	76.2	74.2	Feb 2020
DN2 [2]	92.8	97.8	85.3	85	94.4	92.7	93.1	94.4	95.9	97.3	92.9	Feb 2020
ARAE [44]	72.2	43.1	69.0	55.0	75.2	54.7	70.1	51.0	72.2	40.0	60.2	${\rm Mar}~2020$
GOAD [3]	77.2	96.7	83.3	77.7	87.8	87.8	90.0	96.1	93.8	92.0	88.2	${\rm May}\ 2020$
MahaAD* _{RN101} [41]	92.9	96.4	85.8	85	93.8	91.1	94.1	94.8	95.4	96.8	92.6	${\rm May}\ 2020$
MahaAD* _{ENB4} [41]	95.1	97.8	92.3	91.6	96.5	96.8	97.6	96.9	97.4	98.3	96.0	${\rm May}\ 2020$
HierAD [*] [47]	47.6	63.4	63.2	59.0	79.2	64.3	77.5	66.4	61.6	59.8	64.2	Jun 2020
CSI [53]	89.9	99.9	93.1	86.4	93.9	93.2	95.1	98.7	97.9	95.5	94.3	Jul 2020
Puzzle-AE [45]	78.9	78.1	70.0	54.9	75.5	66.0	74.8	73.3	83.3	70.0	72.5	Aug 2020
PANDA [39]	97.4	98.4	93.9	90.6	97.5	94.4	97.5	97.5	97.6	97.4	96.2	Oct 2020
ConDA [52]	90.9	98.9	88.1	83.1	89.9	90.3	93.5	98.2	96.5	95.2	92.5	Nov 2020
MKD [46]	90.5	90.4	79.7	77.0	86.7	91.4	89.0	86.8	91.5	88.9	87.2	Nov 2020
SSD [50]	82.7	98.5	84.2	84.5	84.8	90.9	91.7	95.2	92.9	94.4	90.0	${\rm Mar}~2021$
SSL [62]	94.8	96.4	88.3	87.6	92.7	94.2	96.4	94.3	96.1	97.0	93.8	May 2021
MTL [32]	84.3	96.0	87.7	82.3	91.0	91.5	91.1	96.3	96.3	92.3	90.9	Jun 2021
MSCL* [40]	97	98.6	94.6	92.2	97.1	96.4	96.5	97.9	98.4	98.6	96.7	Jun 2021
OODformer [27]	92.3	99.4	95.6	93.1	94.1	92.9	96.2	99.1	98.6	95.8	95.7	Jul 2021
DaA [22]	-	-	-	-	-	-	-	-	-	-	75.3	Jul 2021
CFlow* [18]	69.4	83.5	68	73.9	84.7	77.9	84.4	78.6	80.3	84.2	78.5	Jul 2021

Table S3: AUC scores for CIFAR100 experiments of $uni\mbox{-}class.$ * Our results

	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	Mean
Glow* [26]	60.7	59.4	25.4	65.7	45.5	66.9	66.1	46.0	46.0	64.8	75.5	51.1	54.0	48.8	50.6	50.2	52.8	50.1	44.1	53.3	53.8
IC* [51]	61.2	53.9	44.4	44.4	48.3	46.4	41.9	51.2	72.0	58.0	48.7	68.3	69.8	51.6	56.1	62.0	62.4	68.8	59.5	48.8	55.9
OC-SVM [49]	68.4	63.6	52	64.7	58.2	54.9	57.2	62.9	65.6	74.1	84.1	58	68.5	64.6	51.2	62.8	66.6	73.7	52.8	58.4	63.1
DAGMM [65]	43.4	49.5	66.1	52.6	56.9	52.4	55	52.8	53.2	42.5	52.7	46.4	42.7	45.4	57.2	48.8	54.4	36.4	52.4	50.3	50.6
DSEBM [64]	64	47.9	53.7	48.4	59.7	46.6	51.7	54.8	66.7	71.2	78.3	62.7	66.8	52.6	44	56.8	63.1	73	57.7	55.5	58.8
DDV* [31]	58.3	58	70.6	75.3	72.2	60.3	65.4	61.4	63.8	72	77	55.5	82.8	53.4	61.4	58.6	51.9	87.5	64.5	72.3	66.1
HierAD [*] [47]	68.7	59.5	76.5	35.9	59.7	31.6	48.5	59.6	78.4	65.1	76.9	67.6	77.1	55.1	59.1	63.2	69.6	80.1	58.4	57.7	62.4
DVSDD [42]	66	60.1	59.2	58.7	60.9	54.2	63.7	66.1	74.8	78.3	80.4	68.3	75.6	61	64.3	66.3	72	75.9	67.4	65.8	67.0
GOAD [3]	73.9	69.2	67.6	71.8	72.7	67	80	59.1	79.5	83.7	84	68.7	75.1	56.6	83.8	66.9	67.5	91.6	88	82.6	74.5
MHRot [20]	77.6	72.8	71.9	81	81.1	66.7	87.9	69.4	86.8	91.7	87.3	85.4	85.1	60.3	92.7	70.4	78.3	93.5	89.6	88.1	80.1
SSD* [50]	76.5	79.6	88.7	73.4	91.1	72.4	73.9	79.8	80.7	86.0	72.3	79.4	83.1	74.5	87.3	74.4	79.9	90.9	83.3	80.7	80.4
ConDA [52]	82.9	84.3	88.6	86.4	92.6	84.5	73.4	84.2	87.7	94.1	85.2	87.8	82	82.7	93.4	75.8	80.3	97.5	94.4	92.4	86.5
CSI [53]	86.3	84.8	88.9	85.7	93.7	81.9	91.8	83.9	91.6	95	94	90.1	90.3	81.5	94.4	85.6	83	97.5	95.9	95.2	89.6
MKD* [46]	90.3	89.7	90.1	89.9	89.8	90.2	89.7	90.3	90.0	89.5	88.5	90.2	91.0	89.6	89.0	89.8	90.4	88.9	90.1	90.7	89.9
DN2* [2]	88.3	85.6	95.1	95.1	94.4	93.8	94.4	87.3	92.7	91.4	95.8	87.4	88.1	79.3	95.8	78.6	84.1	96.6	91.1	90.4	90.3
PANDA [39]	91.5	92.6	98.3	96.6	96.3	94.1	96.4	91.2	94.7	94	96.4	92.6	93.1	89.4	98	89.7	92.1	97.7	94.7	92.7	94.1
MSCL* [40]	95.8	95.2	97.6	98.3	97.1	96.9	98.3	94.7	97.6	97.9	97.4	96.3	94.9	91.7	98.3	92.7	93.1	98.3	97.9	97.4	96.4
CFlow* [18]	75.3	67.2	76	76	76.6	71.7	76.5	57.9	79.8	83.7	91.5	70.4	74.3	63.1	71.5	64.8	70.3	90.6	64.9	62	73.2
MahaAD* _{RN101} [41]	91.9	89.5	96	95.3	94.7	91.1	95.2	89.5	93.6	93.7	95.4	90.6	91.4	84.3	96.7	84.5	87.7	97.1	94.4	92.8	92.3
MahaAD* _{ENB4} [41]	93.2	92.8	96.7	97.8	97.2	95.4	98.0	92.6	95.9	94.9	95.8	93.0	93.0	89.2	97.8	89.1	91.7	97.5	96.2	94.8	94.6

	CIFAR10:SVHN
CFlow* [18]	6.6
Glow [47]	8.8
DSVDD [42]	14.5
MKD* [46]	26.8
DDV* [31]	47.9
EBM [14]	63.0
DN2* [2]	57.4
VAEBM [60]	83.0
MSCL* [40]	88.3
TT [34]	87.0
LLRe [61]	87.5
BIVA [19]	89.1
NAE [63]	92.0
HierAD [47]	93.9
IC [51]	95.0
GOAD [3]	96.3
SVD-RND [10]	96.4
MHRot [20]	97.8
DoSE [33]	97.3
CSI [53]	99.8
SSD [50]	99.6
MTL [32]	99.9
WAIC [33]	14.3
WAIC [9]	100
MahaAD* _{RN101} [41]	94.3
MahaAD* _{ENB4} [41]	96.2

Table S4: AUC scores for shift-low-res. * Our results

Table S5: AUC scores for *shift-high-res* using Real-A as the in-distribution. QD: quickdraw, IG: infograph, SK: sketch, CA: Clipart, PN: Painting. A is the set without semantic shift, and B with semantic shift. * Our results

Mean
58.3
64.0
48.9
64.0
70.4
59.7
36.9
68.0
61.8
53.6
71.2
75.6

Table S6: AUC scores for *shift-high-res* using $\tt Infograph-A$ as the in-distribution. * Our results

	QDa	QDb	SKa	SKb	REa	REb	CAa	CAb	PNa	PNb	Mean
MSCL* [40]	91.9	91.9	83.9	84.3	92.7	92.8	87.3	86.5	96.3	96.2	90.4
$SSD^{*}[50]$	35.1	33.5	67.9	69.1	56.7	57.7	69.4	69.3	57.3	58.5	57.3
MKD* [46]	83.0	82.4	81.7	80.4	88.9	91.0	84.5	82.5	95.6	95.2	83.0
DDV* [31]	59.5	72.3	56.3	63.4	69.7	75.4	46.6	54.3	70.3	69.9	63.8
DN2* [2]	75.1	75.7	75.1	76.8	82.7	88.1	80.1	79.5	91.2	92.1	81.6
$MHRot^*$ [20]	94.9	95.2	88.5	88.7	87.6	87.9	89.3	89.7	88.6	89.4	86.7
Glow* [26]	0.7	0.6	12.3	14.0	50.7	49.9	35.3	30.6	69.2	69.5	34.4
$IC^{*}[51]$	94.1	94.4	64.8	63.5	42.9	44.8	60.3	62.4	46.7	46.8	61.3
$HierAD^*$ [47]	99.8	99.8	93.8	92.7	83.1	83.3	80.8	83.1	77.6	77.6	84.1
CFlow* [18]	68.8	69	64.9	65.2	74.7	74.9	75.7	75.9	74.5	73.6	71.7
MahaAD* _{RN101} [41]	92.3	92.1	78.1	77.6	88.1	88.4	81.5	80.3	90.9	91.2	86.1
Maha AD^*_{ENB4} [41]	94.5	94.8	89.5	89.0	93.6	94.7	87.4	87.1	94.9	95.4	92.1

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Table S7: AUC scores for $uni\mathcar{-}ano.$ HN is hazelnut, MN is metal nut, TB is toothbrush and TS is transistor. * Our results

	Carpet	Grid	Leather	Tile	Wood	Bottle	Cable	Capsule	HN	MN	Pill	Screw	ΤB	TS	Zipper	Mean
AVID [43]	70	59	58	66	83	88	64	85	86	63	86	66	73	58	84	73
AESSIM [6]	67	69	46	52	83	88	61	61	54	54	60	51	74	52	80	63
AEL2 [6]	50	78	44	77	74	80	56	62	88	73	62	69	98	71	80	71
AnoGAN [48]	49	51	52	51	68	69	53	58	50	50	62	35	57	67	59	55
LSA [1]	74	54	70	70	75	86	61	71	80	67	85	75	89	50	88	73
CAVGA-DU [57]	73	75	71	70	85	89	63	83	84	67	88	77	91	73	87	78
DSVDD [42]	54	59	73	81	87	86	71	69	71	75	77	64	70	65	74	72
VAE-grad [13]	67	83	71	81	89	86	56	86	74	78	80	71	89	70	67	77
GT [15]	46	61.9	82.5	53.9	48.2	74.3	84.8	67.8	33.3	82.4	65.2	44.6	94	79.8	87.4	67.1
Puzzle-AE [45]	65.7	75.4	72.9	65.5	89.5	94.2	87.9	66.9	91.2	66.3	71.6	57.8	97.8	86	75.7	77.6
MKD [46]	79.3	78	95.1	91.6	94.3	99.4	89.2	80.5	98.4	73.6	82.7	83.3	92.2	85.6	93.2	87.7
MSCL* [40]	92.6	53.8	98	97.2	91.2	98.7	88.8	87.4	94.1	85	68.8	63.7	87.5	93.2	96.4	86.4
SSD* [50]	53.4	33.5	61.4	61.9	44.9	78.3	62.7	60.2	62.2	69.4	76.6	59.5	99.8	88.5	74.8	65.8
DDV* [31]	80.3	42	55.1	47.4	46.4	99.7	66.1	77.2	64.2	81	71.9	53.6	64.1	77.8	56	65.5
DN2* [2]	90.3	56.4	98.9	99.2	96.8	99.2	82	84.4	92.9	83.6	69.5	66.4	88.1	91.3	93.8	86.2
MHRot* [20]	47.8	58.9	75	51.2	90.2	82	79.9	59	73.6	75.7	64.9	36.6	86.9	86.5	93.4	70.8
Glow* [26]	72.9	98.3	94.1	83.7	96.9	96.6	83.3	67.1	90.5	62.4	84.8	31.8	87.6	88.4	91.3	82.0
IC* [51]	69.7	75.6	94.3	71.2	78.1	96.0	85.8	63.3	64.9	77.0	67.9	29.7	85.8	89.5	54.9	73.6
HierAD [*] [47]	73.4	95.3	95.5	84.5	97.5	97.3	86.5	70.0	75.0	73.6	74.2	26.2	98.6	92.5	84.1	81.6
SPADE [11]	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	85.5
FAVAE [13]	67.1	97	67.5	80.5	94.8	99.9	95	80.4	99.3	85.2	82.1	83.7	95.8	93.2	97.2	87.9
AEsc [12]	89	97	89	99	95	98	89	74	94	73	84	74	100	91	94	89
DaA [22]	86.6	95.7	86.2	88.2	98.2	97.6	84.4	76.7	92.1	75.8	90	98.7	99.2	87.6	85.9	89.5
CFlow* [18]	99.3	93.3	100	99.2	98.4	99.9	95.5	90.9	99.7	99.5	92.3	83	92.2	93.9	98.7	95.7
MahaAD* _{RN101} [41]	79.5	59.6	99.3	100	98.2	99.3	91.6	93.8	99.4	93.4	90.6	72.1	98.6	96.1	97.9	91.3
$MahaAD^*_{ENB4}$ [41]	98.6	78.8	99.7	100	96.1	99.8	93.5	97.0	99.0	93.9	90.3	78.6	96.7	96.5	97.7	94.4

	OCT	Chest	NIH	DRD1	DRD2	DRD3	DRD4
IF [30]							44.0
AnoGAN [48]							44.2
DSEBM [64]							43.1
DAGMM [65]							52.0
Glow [26]	44.8	54.6					
GT [3]			79.2				
DSVDD [42]	77.4	66.6	81.8				46.4
DeepIF [36]							74.5
DDV [31]	86.7	79.9	57.7	45.3	48.9	50.2	53.4
GAOCC [54]			83.4				
MemDAE [7]			87.8				
$MSCL^*$ [40]	94.1	93.3	81.9	52	55.8	68.2	81.1
$SSD^{*}[50]$	59.4	94.5	74.2	47.5	50.6	54.8	71.4
MKD* [46]	94.9	95.8	88.0	53.7	54.6	60.7	75.5
$DN2^{*}[2]$	94.1	96.9	81.2	54.4	55.6	69.4	85.4
$MHRot^*$ [20]	87.7	96.2	81.8	49.0	50.2	52.7	65.3
$Glow^*$ [26]	62.3	49.8	65.0	52.2	47.5	54.7	59.5
IC* [51]	83.4	91.6	56.7	47.5	52.1	58.2	66.2
$HierAD^*$ [47]	94.3	99.0	79.8	52.1	51.7	57.5	73.5
CFlow* [18]	76.4	81.7	78.7	53.2	55.1	61.3	75.1
MahaAD* _{RN101} [41]	98	99.8	84.6	52.1	52	63.6	79.9
Maha AD^*_{ENB4} [41]	98.7	99.8	84.2	49.9	55.0	66.3	81.3

Table S8: AUC scores for $uni\mbox{-}med.$ * Our results

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