

Polarized Optical-Flow Gyroscope: Supplementary Material

Masada Tzabari and Yoav Y. Schechner

Viterbi Faculty of Electrical Engineering
Technion - Israel Institute of Technology Haifa 32000, Israel
`masada.tz@campus.technion.ac.il ; yoav@ee.technion.ac.il`
<http://www.ee.technion.ac.il/~yoav>

Abstract. This is a supplementary document to the main manuscript. Here we provide a demonstration of angular-velocity estimation from a polarized single-pixel sensor. We also display the polarization and intensity properties of the simulated and experimental scenes.

1 Single-Pixel Sensor

Consider a camera with a wide field of view, but no spatial resolution (a single pixel). A constant rotation rate may be estimated by fitting the change in the single-pixel intensity. Recall Eq. (2) of the main manuscript:

$$I(\mathbf{x}_{\text{cam}}) = I(\mathcal{T}\mathbf{x}_{\text{obj}}) = \frac{c(\mathbf{x}_{\text{obj}})}{2} \{1 + p(\mathbf{x}_{\text{obj}}) \cos 2[\alpha - \theta(\mathbf{x}_{\text{obj}})]\}. \quad (1)$$

Prior to rotation, the polarizer axis is α_0 . Then $\alpha = \alpha_0 + \omega t$. Eq. (1) above becomes

$$I_{\text{cam}} = \frac{c_{\text{obj}}}{2} \left\{ 1 + p_{\text{obj}} \cos 2 \left[\omega t - \tilde{\theta}_{\text{obj}} \right] \right\}, \quad (2)$$

where $\tilde{\theta}_{\text{obj}} = \theta_{\text{obj}} - \alpha_0$. This problem has four unknowns: c_{obj} , p_{obj} , $\tilde{\theta}_{\text{obj}}$, and the angular velocity ω . Therefore, under constant rate of rotation, a solution requires four measurements at different known time instances.

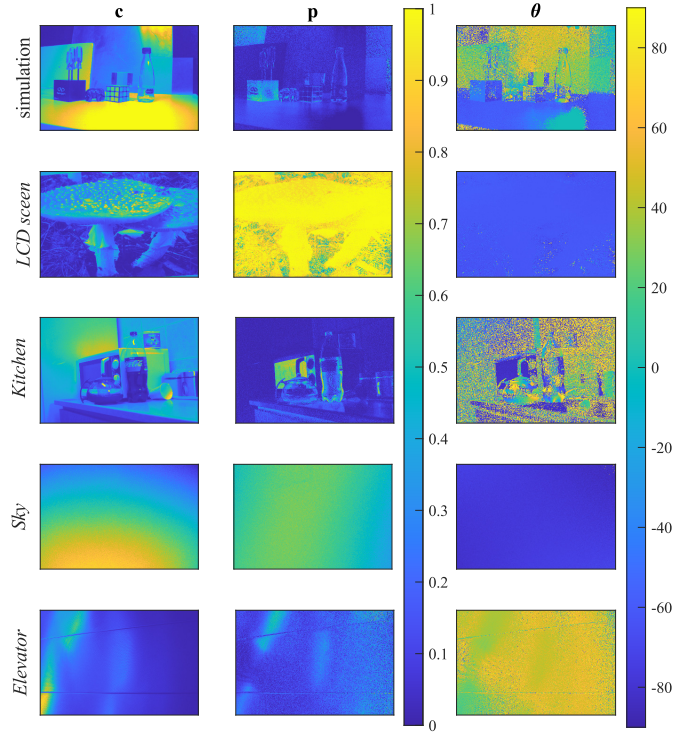
We demonstrate this principle using the experimental images. In lieu of a single wide field pixel, we used the spatial mean intensity of an image. The spatial mean intensity in a sequence of images can be fitted by Least Square (LS) to Eq. (2) above.

$$\{\hat{c}_{\text{obj}}, \hat{p}_{\text{obj}}, \hat{\theta}_{\text{obj}}, \hat{\omega}\} = \underset{c_{\text{obj}}, p_{\text{obj}}, \tilde{\theta}_{\text{obj}}, \omega}{\operatorname{argmin}} \sum_{t=1}^K \left| I_{\text{cam}}(t) - \frac{c_{\text{obj}}}{2} \left\{ 1 + p_{\text{obj}} \cos 2 \left[\omega t - \tilde{\theta}_{\text{obj}} \right] \right\} \right|^2, \quad (3)$$

where $K \geq 4$ is the number of frames. In our case, fitting was done via the MatLab *cftool* curve fitting tool. The true and estimated values of ω are presented in Table 1. Scenes with strong, homogeneous polarization, e.g. *LCD screen* and *Sky*, had more successful estimations.

Table 1. The true values of ω , and values estimated from LS fitting to Eq. (2)

Scene	<i>LCD screen</i>	<i>Kitchen</i>	<i>Sky</i>	<i>Elevator</i>
True ω [deg/frame]	10	6	10	6
estimated ω [deg/frame]	10.18	8.5	7.8	8.6

**Fig. 1.** Polarization and intensity properties of simulated and experimental scenes.

2 Polarization Properties

Fig. 1 presents the ground-truth intensity c , degree of polarization p , and angle of polarization θ , of all simulated and experimental scenes.