

# Fairness by Learning Orthogonal Disentangled Representations (supplementary material)

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## 1 Results in numbers

Table 1: Results on all datasets. Bold face numbers on target task are the highest. Bold numbers in sensitive task are the closest to the majority label classifier.

	CIFAR-10		CIFAR-100		YaleB		Adult		German	
	T	S	T	S	T	S	T	S	T	S
Majority	0.6000	0.1000	0.0500	0.0100	0.0260	0.5056	0.7500	0.6700	0.7100	0.6900
Baseline	0.9775	0.2344	<b>0.7199</b>	0.3069	0.7800	0.9600	0.8500	0.8400	0.8700	0.8000
LFR [7]	-	-	-	-	-	-	0.8230	<b>0.6700</b>	0.7230	0.8050
VAE [3]	-	-	-	-	-	-	0.8190	0.6600	0.7250	0.7950
VFAE [4]	-	-	-	-	0.8500	0.5700	0.8130	<b>0.6700</b>	0.7270	0.7970
Xie et al. [6] (trade-off #1)	0.9752	0.2083	0.7132	0.1543	0.8900	0.5700	0.8440	0.6770	0.7440	0.8020
Roy et al. [5] (trade-off #1)	<b>0.9778</b>	0.2344	0.7117	0.1688	0.8900	0.4000	0.8460	0.6550	<b>0.8633</b>	0.7270
Xie et al. [6] (trade-off #2)	0.9735	0.2064	0.704	0.1484	-	-	-	-	-	-
Roy et al. [5] (trade-off #2)	0.9679	0.2114	0.705	0.1643	-	-	-	-	-	-
Ours	0.9725	<b>0.1907</b>	0.7074	<b>0.1447</b>	<b>0.8923</b>	<b>0.5292</b>	<b>0.8520</b>	0.6826	0.7700	<b>0.7100</b>

## 2 Biased categories accuracy

Biased categories accuracy reported in [6] which represents the target accuracy of the biased sensitive group. It is used as an indicator of how well the model performs on minority classes. The closer the biased accuracy to the overall accuracy, the better the model is in terms of fairness. The results are shown in Table. 2

## 3 Implementation details

*Extended YaleB dataset:* For the Extended YaleB dataset, we use an experimental setup similar to Xie *et al.* [6] and Louizos *et al.* [4] by using the same

Table 2: Biased categories accuracy on three datasets

	<b>Entropy + KL Orth.</b>		<b>w/o Entropy w/o KL</b>	
<b>Dataset</b>	<b>Overall</b>	<b>Biased</b>	<b>Overall</b>	<b>Biased</b>
Adult	0.8520	0.8157	0.8494	0.8108
German	0.77	0.7241	0.7433	0.6897
Yale	0.8923	0.5867	0.8650	0.4933

train/test split strategy. We used  $38 \times 5 = 190$  samples for training and 1096 for testing. The model setup is similar to [6, 5], the encoder consisted of one layer, target predictor is one linear layer and the discriminator is neural network with two hidden layers each contains 100 units. The parameters are trained using Adam optimizer with a learning rate of  $10^{-4}$  and weight decay of  $5 \times 10^{-2}$ . For the extended YaleB dataset we set  $\lambda_{OD} = 0.037$ ,  $\lambda_E = 1.0$ ,  $\gamma_{OD} = 1.1$ ,  $\gamma_E = 2.0$ ,  $d_T = d_S = 100$ .

*CIFAR datasets:* Similar to [5], we employed ResNet-18 [1] architecture for training the encoder on the two CIFAR datasets. For the discriminator and target classifiers, we employed a neural network with two hidden layers (256 and 128 neurons). For the encoder, we set the learning rate to  $10^{-4}$  and weight decay to  $10^{-2}$ . For the target and discriminator networks, the learning rate and weight decay were set to  $10^{-2}$  and  $10^{-3}$ , respectively. Adam optimizer [2] is used in all experiments. For the CIFAR-10 dataset we set  $\lambda_{OD} = 0.063$ ,  $\lambda_E = 1.0$ ,  $\gamma_{OD} = 1.7$ ,  $\gamma_E = 1$ ,  $d_T = d_S = 128$ . For the CIFAR-100 dataset we set  $\lambda_{OD} = 0.0325$ ,  $\lambda_E = 0.1$ ,  $\gamma_{OD} = 1.2$ ,  $\gamma_E = 1.67$ ,  $d_T = d_S = 128$ .

*Tabular datasets:* For the Adult and German datasets, we follow the setup appeared in [5] by having a 1-hidden-layer neural network as encoder, the discriminator has two hidden layer and the target predictor is a logistic regression layer. Each hidden layer contains 64 units. The size of the representation is 2. The learning rate for all components is  $10^{-3}$  and weight decay is  $5 \times 10^{-4}$ . For the Adult dataset we set  $\lambda_{OD} = 0.037$ ,  $\lambda_E = 0.55$ ,  $\gamma_{OD} = 0.8$ ,  $\gamma_E = 1.66$ ,  $d_T = d_S = 2$ . For the German dataset we set  $\lambda_{OD} = 0.01$ ,  $\lambda_E = 1.0$ ,  $\gamma_{OD} = 1.4$ ,  $\gamma_E = 2.0$ ,  $d_T = d_S = 2$ .

## 4 Sensitivity analysis heatmaps

## References

1. He, K., Zhang, X., Ren, S., Sun, J.: Identity mappings in deep residual networks. In: European Conference on Computer Vision. pp. 630–645. Springer (2016)
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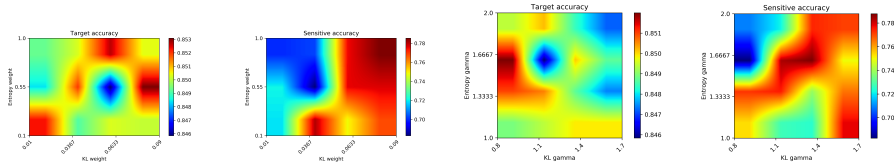


Fig. 1: Sensitivity analysis on the Adult dataset

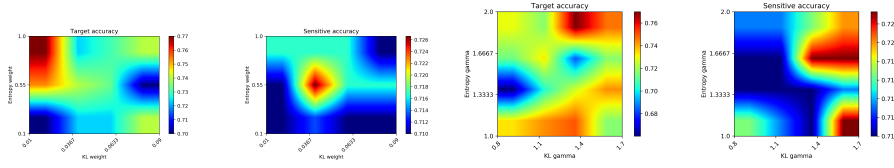


Fig. 2: Sensitivity analysis on the German dataset

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4. Louizos, C., Swersky, K., Li, Y., Welling, M., Zemel, R.: The variational fair autoencoder. arXiv preprint arXiv:1511.00830 (2015)
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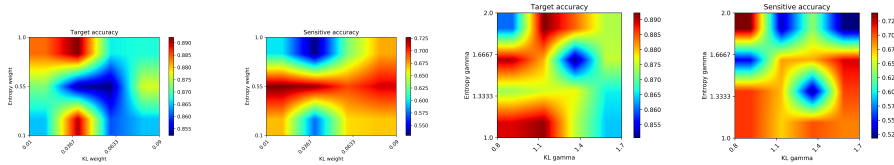


Fig. 3: Sensitivity analysis on the extended YaleB dataset