

Supplementary File to “Unfolded Deep Kernel Estimation for Blind Image Super-resolution”

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In this supplementary file, we provide the following materials:

- Network architectures of $\text{Net}_{\mathbf{X}}$, $\text{Net}_{\mathbf{K}}$ and HypaNet (referring to Section 3.3 and Section 3.4 in the main paper).
- The $\times 3$ BISR results with DEPD-evaluation pool (referring to Section 4.2 in the main paper).
- The BISR results on several selected kernels from the DEPD-evaluation pool (referring to Section 4.2 in the main paper).
- More visualization of kernels estimated by UDKE and other kernel estimation methods (referring to Section 4.2 in the main paper).
- The BISR Results with isotropic Gaussian kernels (referring to Section 4.2 in the main paper).
- Visualization of the outputs in each stage of UDKE (referring to Section 4.2 in the main paper).
- More visualization results of BISR with DEPD kernel pool (referring to Section 4.2 in the main paper).
- More visualization results of BISR on real-world low-resolution images (referring to Section 4.2 in the main paper).

1 Network Architectures of $\text{Net}_{\mathbf{X}}$, $\text{Net}_{\mathbf{K}}$ and HypaNet

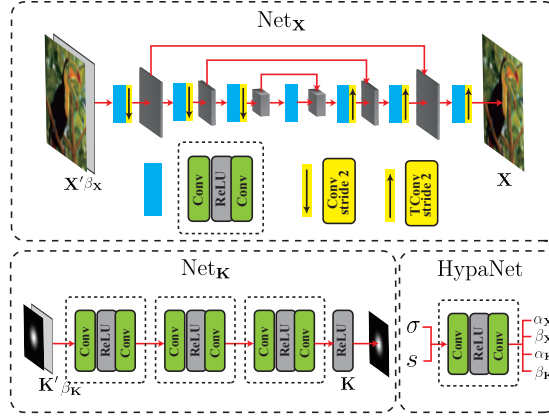
Fig. 1 shows the network architectures of $\text{Net}_{\mathbf{X}}$, $\text{Net}_{\mathbf{K}}$ and HypaNet.

2 $\times 3$ BISR Results with DEPD-evaluation Pool

Table 1 shows the experimental results of $\times 3$ BISR results with DEPD-evaluation pool. Table 2 shows the kernel estimation results. Note that some methods cannot be applied to $3\times$ SR and thus they are omitted. It can be seen that UDKE based BISR method achieves the highest BISR and kernel estimation performance.

3 BISR Results on Selected DEPD-evaluation Kernels

Table 3 shows the BISR results on some distinct kernels selected from the DEPD-evaluation pool. The experiment is done on BSD100 images with $s=2$ and $\sigma=7.65$. It can be seen that UDKE based BISR framework consistently shows the SOTA performance on different testing blur kernels.

Fig. 1: Network architectures of Net_X , Net_K and HypaNet.

Datasets	Set5			BSD100			Urban100		
σ	0	2.55	7.65	0	2.55	7.65	0	2.55	7.65
Bicubic	24.56/7570	24.51/7463	24.12/6819	23.61/6329	23.56/6243	23.23/5684	20.80/6258	20.76/6163	20.62/5601
RCAN	25.26/7911	25.13/7582	23.94/6680	23.90/7209	23.73/6826	21.43/5088	21.89/6791	21.65/6788	20.01/5020
ZSSR	25.22/7810	24.71/7419	23.47/6213	24.10/7464	23.91/7098	21.29/4971	22.66/7043	22.34/6921	21.09/5179
DASR	25.97/8110	25.37/7833	23.91/6452	24.62/7552	24.55/7254	21.65/5149	22.71/7350	22.37/7152	20.94/5016
DFKP	25.51/7825	25.03/7512	22.32/5917	23.79/7343	23.62/7043	20.03/4543	20.31/7040	19.98/6949	19.02/4654
IKC	24.98/7656	24.81/7413	24.01/6690	24.21/7460	24.07/7154	21.87/5029	22.05/7032	21.68/7010	20.77/5025
DAN	25.80/8012	25.22/7637	23.88/6170	24.42/7554	24.31/7213	21.65/5289	22.71/7335	22.48/7227	20.65/5230
Ours	29.12/8617	28.92/8478	27.86/8161	26.19/7768	26.04/7426	25.43/6999	24.02/7715	23.92/7630	23.56/7416
UBound	32.61/9004	32.23/8711	31.10/8537	29.22/8313	29.02/7870	28.45/7636	27.99/8010	26.89/7862	26.42/7260

Table 1: $3\times$ BISR results (PSNR/SSIM). Best results are in red.

Scale	Datasets	Set5			BSD100			Urban100		
$\times 3$	σ	0	2.55	7.65	0	2.55	7.65	0	2.55	7.65
	DFKP	39.2	39.0	37.8	38.7	38.2	37.5	37.2	37.2	37.0
	Ours	46.8	47.0	45.5	47.1	46.7	45.1	47.3	47.0	46.1

Table 2: Kernel estimation results (PSNR). Best results are in red.

4 More Visualization of Estimated Kernels

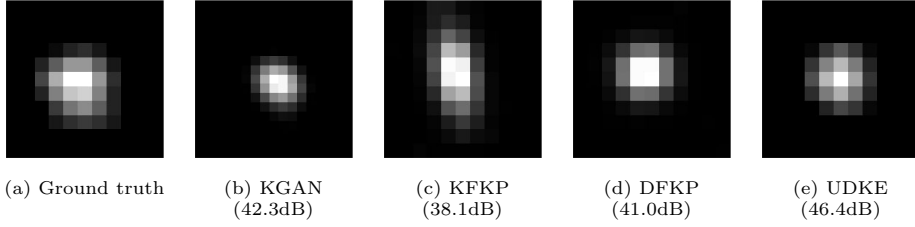
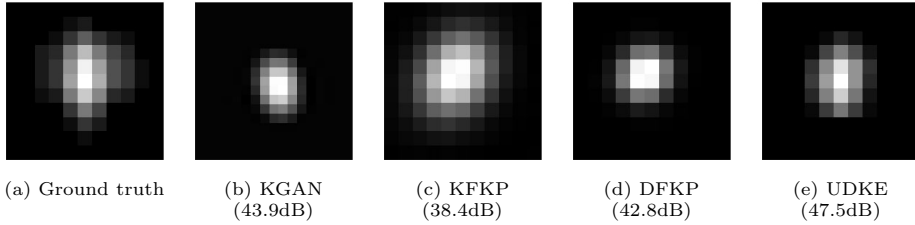
Figs. 2~3 show more visualization of kernels estimated by UDKE and other kernel estimation methods. It can be seen that UDKE produces more reliable estimation of unseen blur kernels during inference.

5 BISR Results with Isotropic Gaussian Kernels

Table 4 shows the BISR results with isotropic Gaussian kernels. It can be seen that UDKE achieves competitive results with those BISR methods specifically

									
Bicubic	24.52/6411	24.58/6025	24.02/6123	24.04/6433	24.85/6768	24.44/6328	24.52/6470	24.03/5979	24.68/6708
RCAN	23.72/5365	23.23/5165	23.47/5359	23.01/5011	23.67/5235	23.43/5109	23.73/5498	23.13/5298	23.86/5525
ZSSR	24.71/6834	25.02/7043	25.24/7323	24.83/7233	24.89/7310	25.20/7321	24.99/7432	25.45/7236	25.20/7235
DASR	24.01/5632	23.92/5594	23.45/5293	23.77/5695	23.99/5860	23.04/5202	23.57/5905	23.77/5342	23.12/5231
KGAN	18.45/3928	18.14/3948	18.83/3485	18.10/3101	18.62/3290	18.54/3123	18.65/3483	18.04/2982	18.55/3342
KFKP	16.32/2985	16.10/2583	16.75/2685	16.12/2950	16.01/2409	16.47/2938	16.73/2192	16.95/2940	15.94/2394
DFKP	20.18/3711	19.57/3634	19.85/3621	20.01/3582	20.13/3364	19.03/3531	19.85/3651	20.10/3427	19.57/3922
IKC	25.10/7343	25.12/7256	25.01/7074	25.32/7368	25.03/7266	24.98/6950	25.23/7654	25.09/7079	25.20/7354
DAN	23.62/5543	23.15/5125	23.54/5540	23.92/5783	23.11/5089	23.62/5798	23.35/5610	23.80/5910	23.88/5910
Ours	26.56/7636	26.54/7591	26.19/7397	25.41/7052	26.56/7607	26.61/7635	26.67/7702	25.14/7046	26.66/7673
UBound	28.01/8409	27.96/8520	27.85/8254	27.67/8175	28.00/8508	27.77/8243	27.91/8378	27.53/8165	28.12/8680

Table 3: BISR results (PSNR/SSIM) on different kernels. Best results are in red.

Fig. 2: Kernel estimation results by different methods on “baby” in Set5 with $s=3$ and $\sigma=2.55$.Fig. 3: Kernel estimation results by different methods on “img051” in Urban100 with $s=4$ and $\sigma=7.65$.

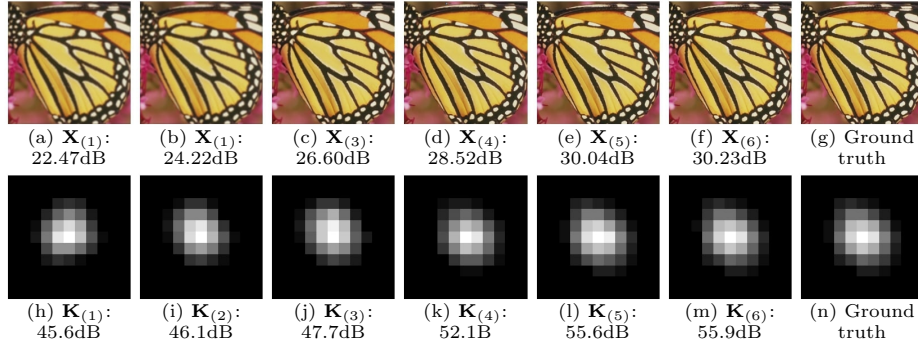
designed for Gaussian kernels but without hardcoding any Gaussian priors, and it achieves the best performance when the noise increases.

6 Outputs in Each Stage of UDKE

Fig. 4 shows the outputs in each stage of UDKE. It can be seen that UDKE progressively improves the estimations of BISR kernel and super-resolution results, which validates the motivation and effectiveness of our architecture design.

s		$\sigma=0$	$\sigma=2.55$	$\sigma=7.65$
2	DAN	29.78/8531/-	29.25/8358/-	28.31/7510/-
	KGAN	29.76/8420/47.9	29.13/7378/46.5	28.10/7026/45.8
	KFKP	29.79/8530/49.4	29.27/8429/47.1	28.24/7450/46.2
	DFKP	30.12/8940/49.8	29.40/8611/47.4	28.45/7570/46.2
	Ours	29.80/8522/48.8	29.24/8435/47.0	28.57/7700/46.4
4	DAN	26.34/7849/-	25.92/7320/-	25.42/5820/-
	KGAN	26.21/7810/46.2	25.73/7243/44.2	25.30/5575/41.9
	KFKP	26.48/7911/46.3	25.94/7310/44.9	25.43/5801/42.4
	DFKP	26.53/8012/47.5	26.10/7592/45.3	25.68/6013/44.4
	Ours	26.43/7834/46.2	25.98/7324/44.8	25.72/6187/44.5

Table 4: BISR results (PSNR/SSIM/Kernel-PSNR) on isotropic Gaussian kernels.

Fig. 4: Outputs in each stage of UDKE on “butterfly” in Set5 with $s=2$ and $\sigma=0$.

7 More Visualization Results of BISR with DEPD Kernel Pool

Figs. 5~12 visualize the BISR results with DEPD kernel pool. It can be seen that UDKE generally recovers richer and clearer textures (see Figs. 7 and 12) and it is more robust to noisy images (see Figs. 5, 9, 10).

8 More Visualization Results of BISR on Real-world Images

Figs. 13~18 visualizes the BISR results on real-world images. Note that KGAN, KGAN-FKP, BSRGAN, and RESRGAN cannot be applied to $3\times$ super-resolution so that their results are not shown for $3\times$ BISR. One can see that UDKE can reproduce much sharper edges and clearer textures without falsely changing their original patterns.

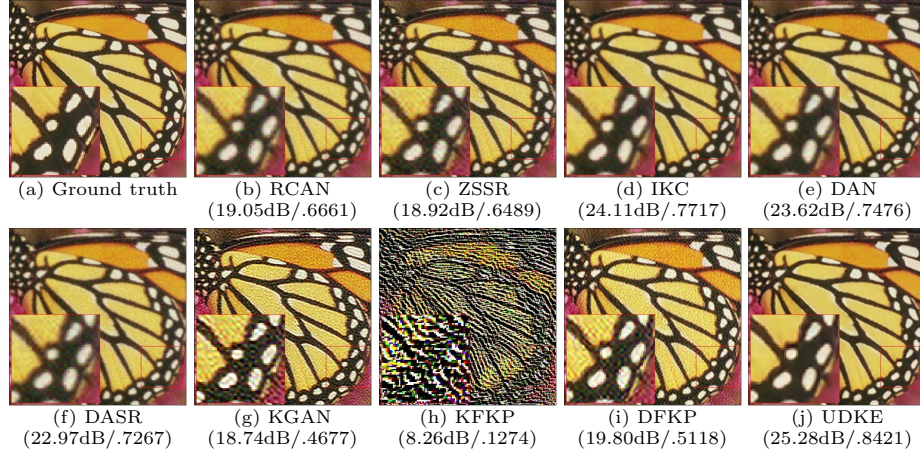


Fig. 5: BISR results (PSNR/SSIM) on “butterfly” in Set5 with $s=2$ and $\sigma=7.65$.

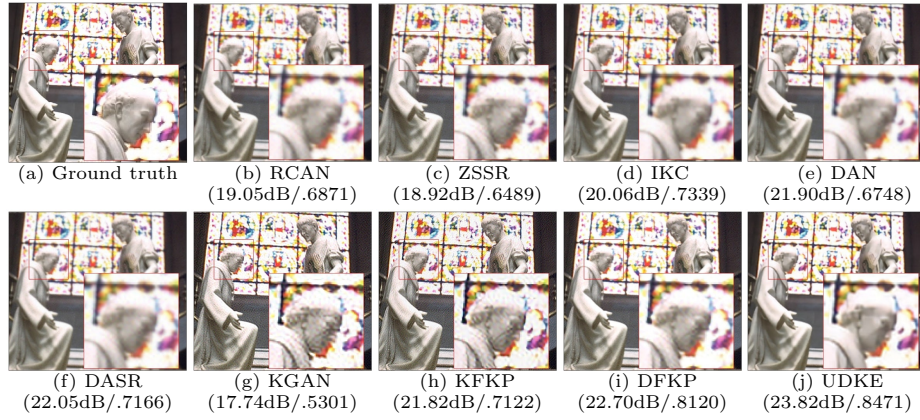


Fig. 6: BISR results (PSNR/SSIM) on “24077” in BSD100 with $s=2$ and $\sigma=2.55$.

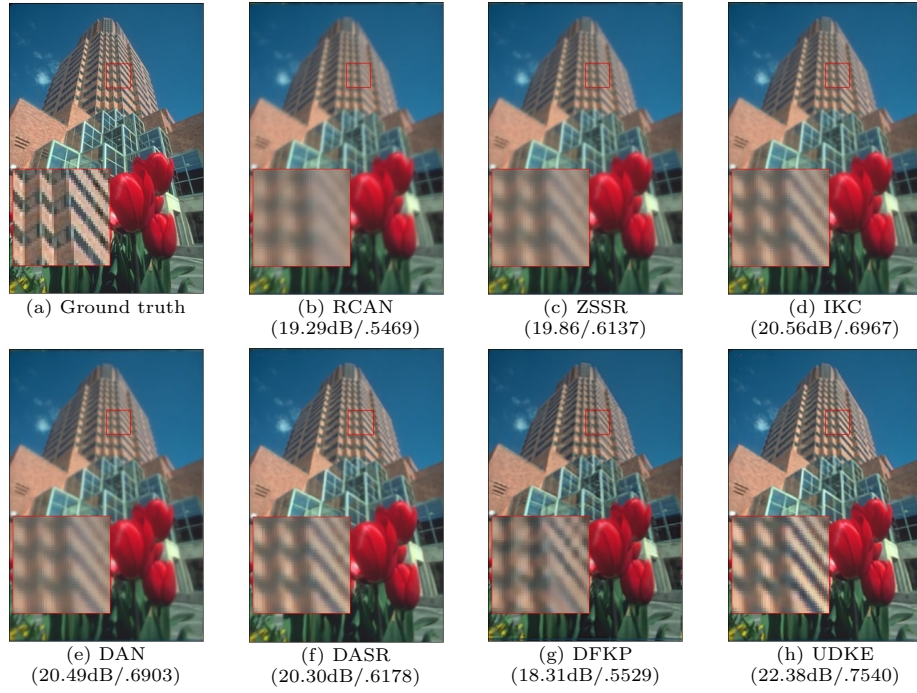


Fig. 7: BISR results (PSNR/SSIM) on “86000” in BSD100 with $s=3$ and $\sigma=0$.

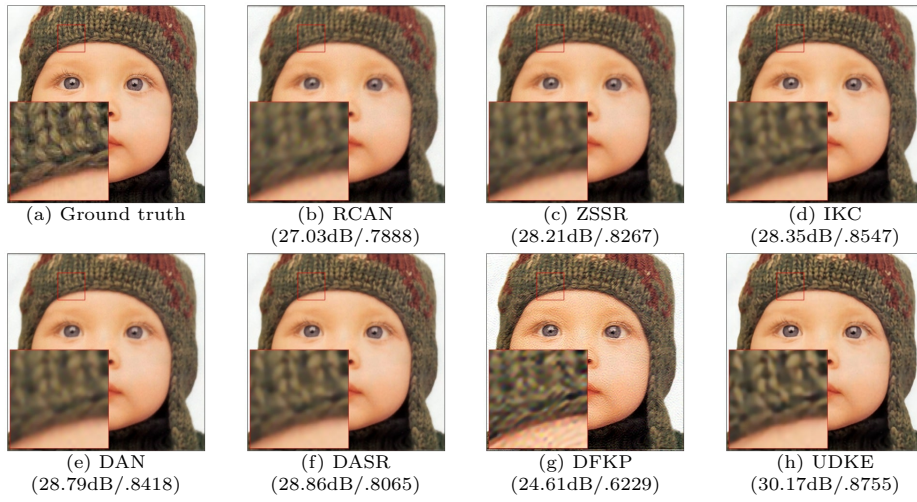


Fig. 8: BISR results (PSNR/SSIM) on “baby” in Set5 with $s=3$ and $\sigma=2.55$.

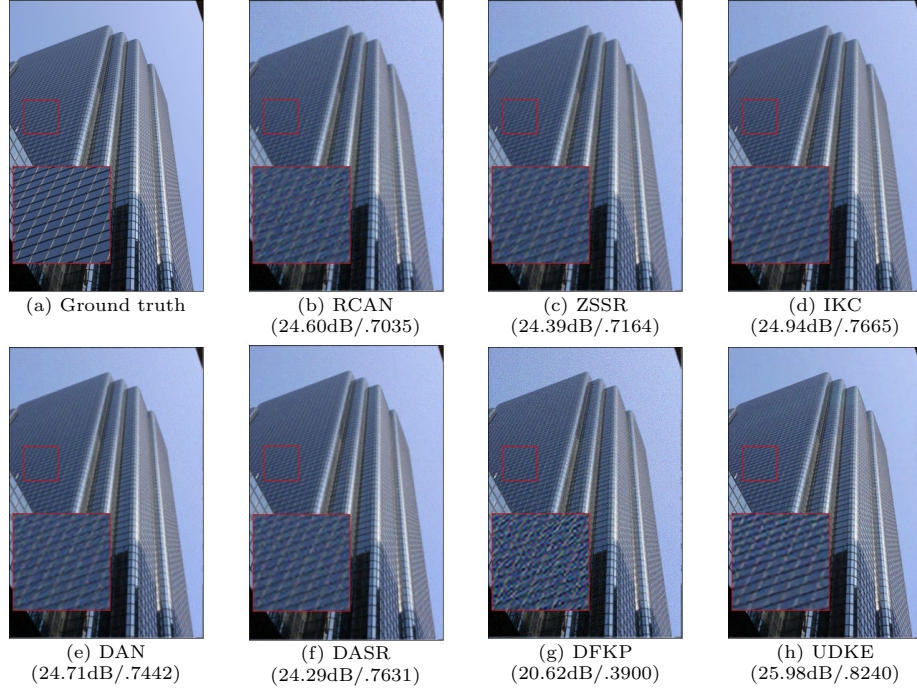


Fig. 9: BISR results (PSNR/SSIM) on “074” in Urban100 with $s=3$ and $\sigma=7.65$.

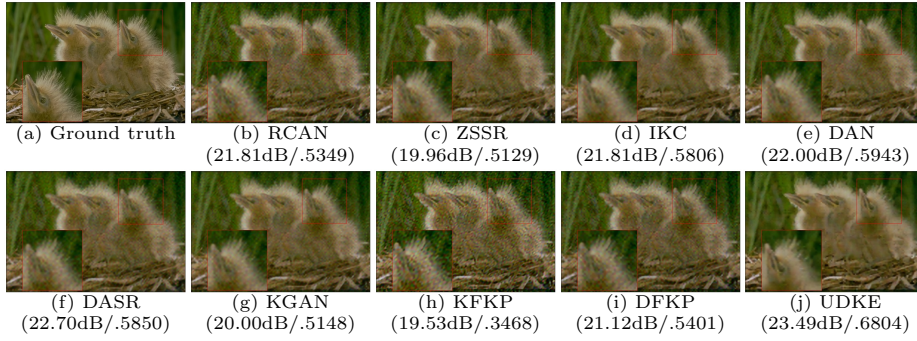
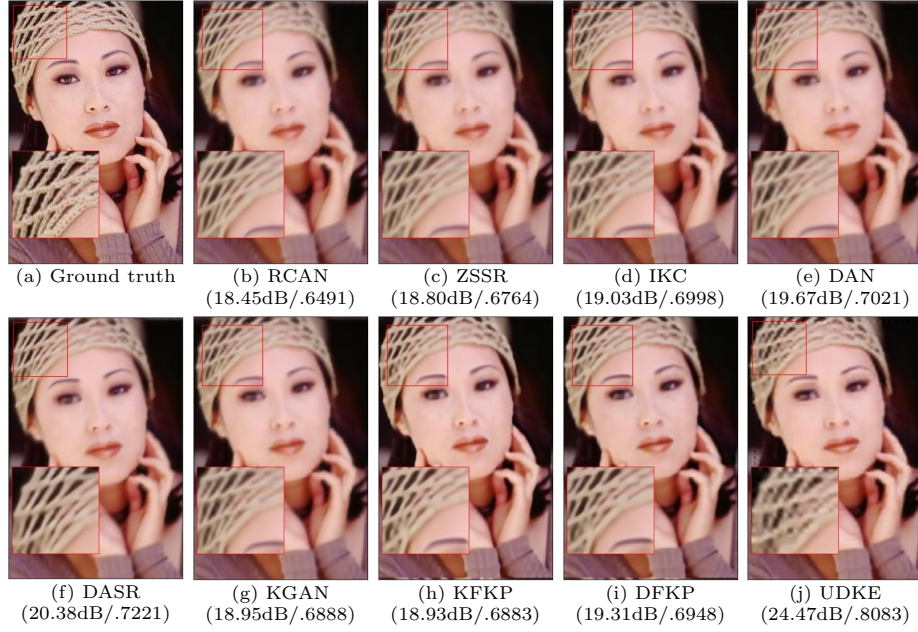
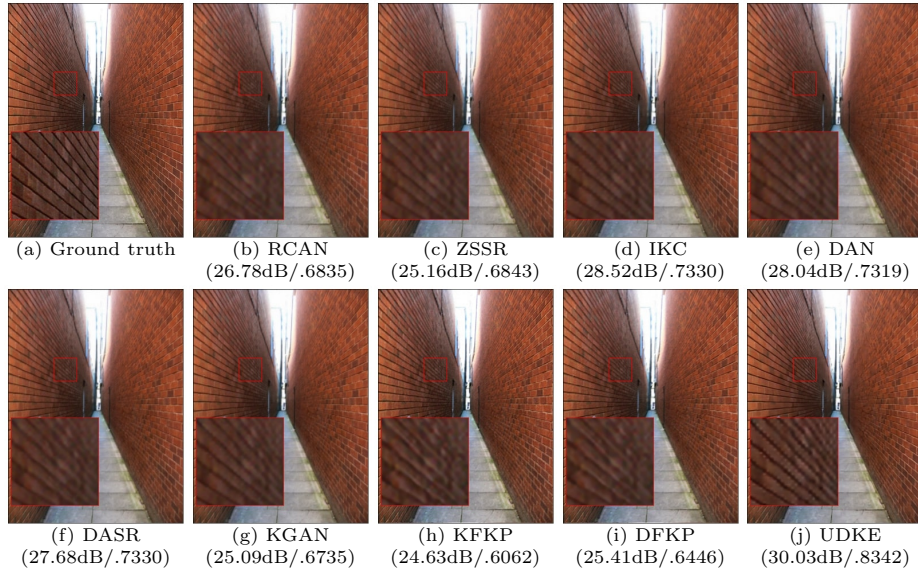
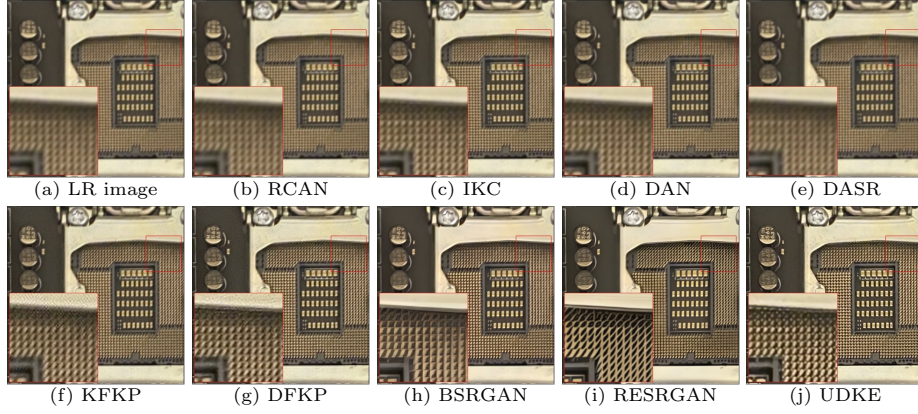
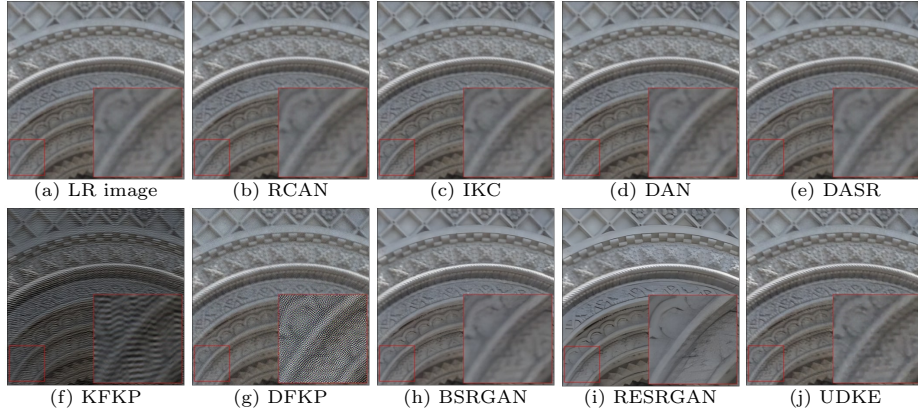
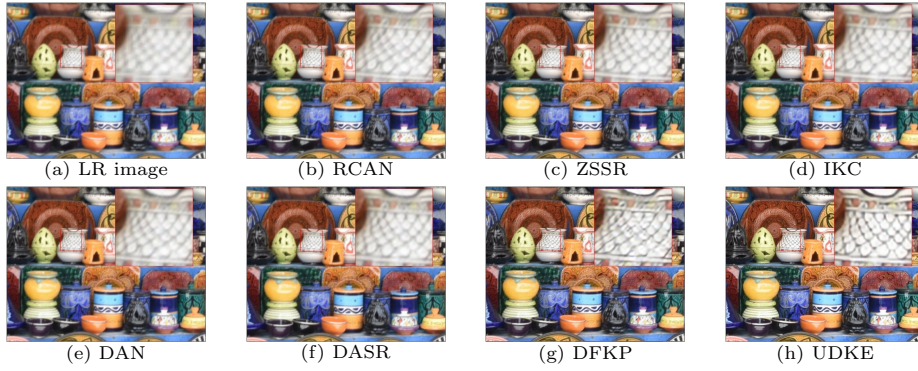


Fig. 10: BISR results (PSNR/SSIM) on “163085” in BSD100 with $s=4$ and $\sigma=7.65$.

Fig. 11: BISR results (PSNR/SSIM) on “woman” in Set5 with $s=4$ and $\sigma=0$.Fig. 12: BISR results (PSNR/SSIM) on “038” in Urban100 with $s=4$ and $\sigma=2.55$.

Fig. 13: $\times 2$ BISR results on a real-world image (better viewed on screen).Fig. 14: $\times 2$ BISR results on a real-world image (better viewed on screen).Fig. 15: $\times 3$ BISR results on a real-world image (better viewed on screen).

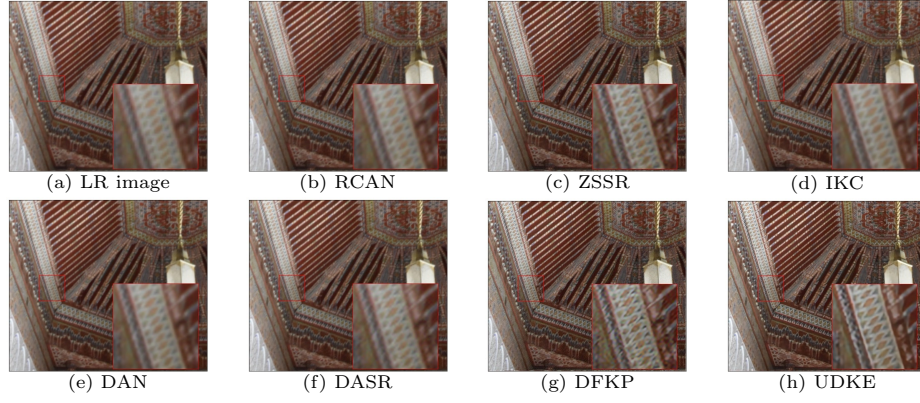


Fig. 16: $\times 3$ BISR results on a real-world image (better viewed on screen).

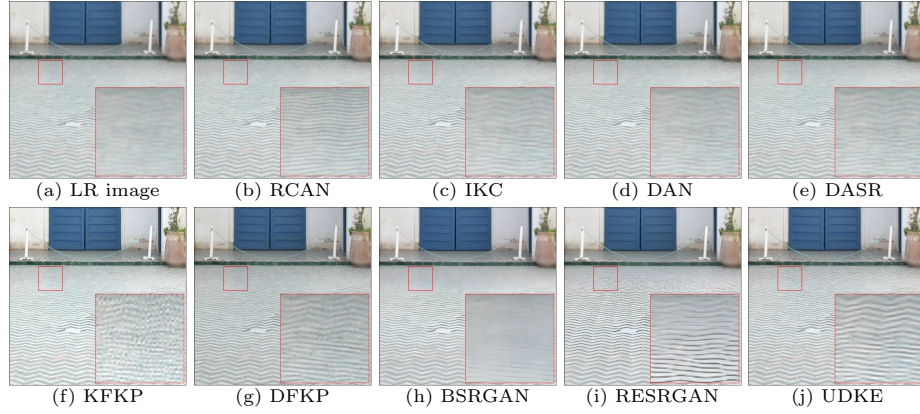


Fig. 17: $\times 4$ BISR results on a real-world image (better viewed on screen).

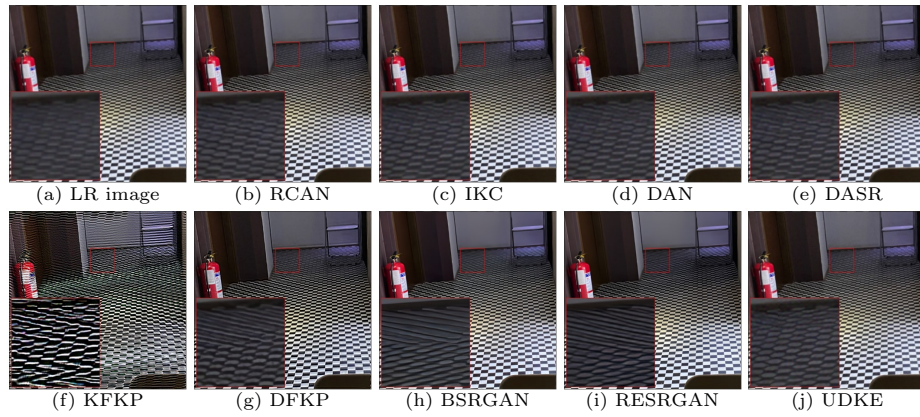


Fig. 18: $\times 4$ BISR results on a real-world image (better viewed on screen).