

6 Appendix

6.1 Code Release & Implementation details

FedX is open-sourced at <https://github.com/Sungwon-Han/FEDX>. Algorithm 1 shows the overall training process.

Algorithm 1 Local update process of FedX

Input: the number of local epochs E , global model F , local model f^m , projection head h^m , local dataset \mathcal{D}^m , and temperature τ
Output: a trained local model f^m and a projection head h^m

In each client m ,

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 $f^m \leftarrow F$  // Replace the local model with the global model
 $F \leftarrow F.detach()$  // Fix the global model for a given communication round
for epoch  $e \in \{1, 2, \dots, E\}$  do
  for batch  $\mathcal{B}, \mathcal{B}_r \in \mathcal{D}^i$  do
     $\tilde{\mathcal{B}} \leftarrow \text{Augment}(\mathcal{B})$ 
    for  $\mathbf{x}_i \in \mathcal{B}, \tilde{\mathbf{x}}_i \in \tilde{\mathcal{B}},$  and  $\mathbf{x}_j \in \mathcal{B}_r$  do
      /* Local KD */ /* Global KD */
       $\mathbf{z}_i, \mathbf{z}_j, \tilde{\mathbf{z}}_i \leftarrow f^m(\mathbf{x}_i), f^m(\mathbf{x}_j), f^m(\tilde{\mathbf{x}}_i)$ 
       $\mathbf{z}_i^l, \tilde{\mathbf{z}}_i^l \leftarrow h^m \circ f^m(\mathbf{x}_i), h^m \circ f^m(\tilde{\mathbf{x}}_i)$ 
       $\mathbf{z}_i^g, \mathbf{z}_j^g, \tilde{\mathbf{z}}_i^g \leftarrow F(\mathbf{x}_i), F(\mathbf{x}_j), F(\tilde{\mathbf{x}}_i)$ 

      // Local relationship vectors // Global relationship vectors
       $\mathbf{r}_i^j = \frac{\exp(\text{sim}(\mathbf{z}_i, \mathbf{z}_j)/\tau)}{\sum_{k \in \mathcal{B}_r} \exp(\text{sim}(\mathbf{z}_i, \mathbf{z}_k)/\tau)}$ 
       $\mathbf{r}_i'^j = \frac{\exp(\text{sim}(\mathbf{z}_i^l, \tilde{\mathbf{z}}_i^g)/\tau)}{\sum_{k \in \mathcal{B}_r} \exp(\text{sim}(\mathbf{z}_i^l, \mathbf{z}_k^g)/\tau)}$ 
       $\tilde{\mathbf{r}}_i^j = \frac{\exp(\text{sim}(\tilde{\mathbf{z}}_i, \mathbf{z}_j)/\tau)}{\sum_{k \in \mathcal{B}_r} \exp(\text{sim}(\tilde{\mathbf{z}}_i, \mathbf{z}_k)/\tau)}$ 
       $\tilde{\mathbf{r}}_i'^j = \frac{\exp(\text{sim}(\tilde{\mathbf{z}}_i^l, \mathbf{z}_j^g)/\tau)}{\sum_{k \in \mathcal{B}_r} \exp(\text{sim}(\tilde{\mathbf{z}}_i^l, \mathbf{z}_k^g)/\tau)}$ 

       $L_c^{\text{local}} \leftarrow \text{Calculate from Eq. 3 or 5}$ 
       $L_c^{\text{global}} \leftarrow \text{Calculate from Eq. 9}$ 
       $L_r^{\text{local}} \leftarrow \text{Calculate from Eq. 7}$ 
       $L_r^{\text{global}} \leftarrow \text{Calculate from Eq. 11}$ 
       $L_{\text{local-KD}} = L_c^{\text{local}} + L_r^{\text{local}}$ 
       $L_{\text{global-KD}} = L_c^{\text{global}} + L_r^{\text{global}}$ 
    end
     $L_{\text{total-KD}} = L_{\text{local-KD}} + L_{\text{global-KD}}$  // Calculate the total loss
    Update  $f^m, h^m$  via back-propagation // Update local model parameters
  end
end
return  $f^m, h^m$ 

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6.2 Further Results on Performance Evaluation

Statistical errors in Table 1. Table 5 reports standard errors from various training iterations (i.e., last five epochs & best five epochs), which shows that our model’s accuracy converges stably.

Table 5: Adding FedX increases the performance of various federate learning models. The final round accuracy and the best accuracy are reported with standard errors.

Method	CIFAR-10		SVHN		F-MNIST	
	Last	Best	Last	Best	Last	Best
FedSimCLR	51.31±0.25	52.88±0.06	75.19±3.14	76.50±0.04	77.66±0.75	79.44±0.06
+ FedX	56.88±0.72	57.95±0.03	77.19±1.67	77.70±0.09	81.98±0.74	82.47±0.02
FedMoCo	56.74±1.63	57.82±0.02	70.69±3.03	70.99±0.07	82.31±0.18	83.58±0.06
+ FedX	58.23±1.22	59.43±0.09	73.57±2.79	73.92±0.02	83.62±0.32	84.65±0.04
FedBYOL	52.24±0.61	53.14±0.06	65.95±1.62	67.32±0.24	81.45±0.27	82.37±0.06
+ FedX	56.49±0.72	57.79±0.12	68.94±1.13	69.05±0.07	83.18±0.31	84.30±0.07
FedProtoCL	51.33±1.03	52.12±0.03	49.85±0.77	50.19±0.11	81.76±0.22	83.57±0.04
+ FedX	55.36±0.98	56.76±0.01	69.31±1.72	69.75±0.15	82.74±0.35	83.34±0.04
FedU	50.79±0.47	50.79±0.05	66.02±1.83	66.22±0.17	80.59±0.42	82.03±0.05
+ FedX	56.15±0.58	57.26±0.05	68.13±1.17	68.39±0.07	83.73±0.20	84.12±0.03

Table 6: Performance improvement with three different algorithms on classification accuracy. Both the final round accuracy and the best accuracy show that FedX brings nontrivial improvement over the baseline algorithm.

Method	CIFAR-10		SVHN		F-MNIST	
	Last	Best	Last	Best	Last	Best
FedSimCLR	51.31	52.88	75.19	76.50	77.66	79.44
+ FedCA	47.46	48.54	59.40	59.86	81.51	82.05
+ MOON-unsup	51.78	52.84	75.36	76.03	80.58	80.93
+ FedX (ours)	56.88	57.95	77.19	77.70	81.98	82.47

Table 7: Performance improvement on ImageNet-10. Both last and best round accuracy are reported.

Method	FedSimCLR		FedSimCLR+FedX	
	Last	Best	Last	Best
ImageNet-10	81.50	81.50	86.17	86.57

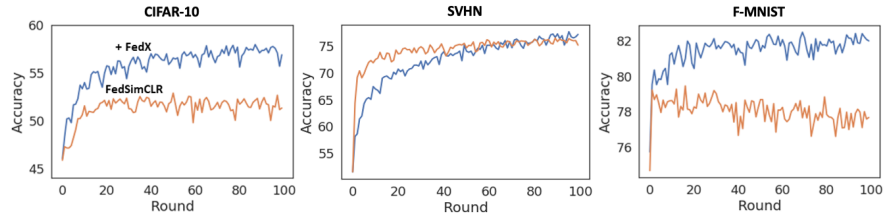
Comparison with other relevant baselines. We compared FedX with other contrastive learning methods: FedCA (Zhang *et al.*)⁶ and MOON (Li *et al.*). We followed the same implementation guidelines as in the original work, only substituting the InfoNCE objective for the supervised loss in MOON (calling this MOON-unsup). FedSimCLR with FedAvg served as the base framework in both cases. Our method continues to outperform, as shown in Table 6, demonstrat-

⁶ Note that the dictionary module has been removed from FedCA for fair comparison as it directly shares the local data information of all clients.

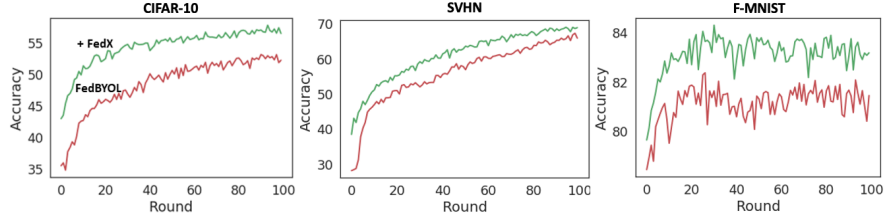
ing the benefit of the proposed knowledge distillation strategy in unsupervised federated learning.

Performance on ImageNet. To verify our model’s applicability to the large-scale dataset, we run FedX on ImageNet-10 benchmark, a 10-class subset of ImageNet. FedX was trained for 10 local epochs in each communication round, with a total of 50 rounds. Table 7 shows that adding FedX to FedSimCLR improves the classification accuracy by 5pp. Extended results for the larger number of the class will also be released.

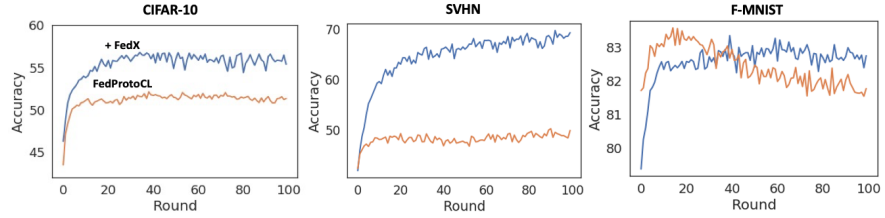
Full comparison results over communication rounds. FedX brings meaningful performance improvements than when using the baseline algorithms alone. Figure 7 shows trajectories including three additional baselines – FedProtoCL, FedMoCo, and FedU that were omitted in Fig. 4. We can check how quickly the model benefits baselines over the varying communication rounds. Especially, in FedSimCLR and FedProtoCL (F-MNIST) experiments, FedX prevents the local bias degrading the performance during the entire training phase and thereby stops such deterioration in performance.



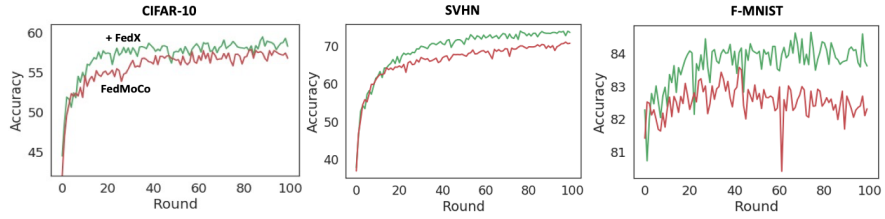
(a) Performance gain on FedSimCLR



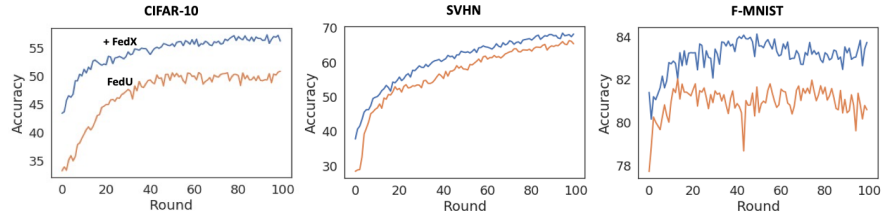
(b) Performance gain on FedBYOL



(c) Performance gain on FedProtoCL



(d) Performance gain on FedMoCo



(e) Performance gain on FedU

Fig. 7: Performance comparison between all baselines (i.e., FedSimCLR, FedBYOL, FedProtoCL, FedMoCo, and FedU) and FedX-enhanced versions over communication rounds. FedX brings extra performance on baseline unsupervised learning models in three benchmark datasets.